


Kinetic modeling of collective behavior: When a good match goes bad



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Overview

Artificial Successes

Superficial Matches

New Hopes

Conclusions

Overview

Artificial Successes

Allocation Kinetics

Superficial Matches

Collective Transport

Swarm Assembly

New Hopes

Drift–Diffusion Decision-Making

Conclusions

Collective Transport

Decentralized Organization of Teams Carrying Loads

Overview

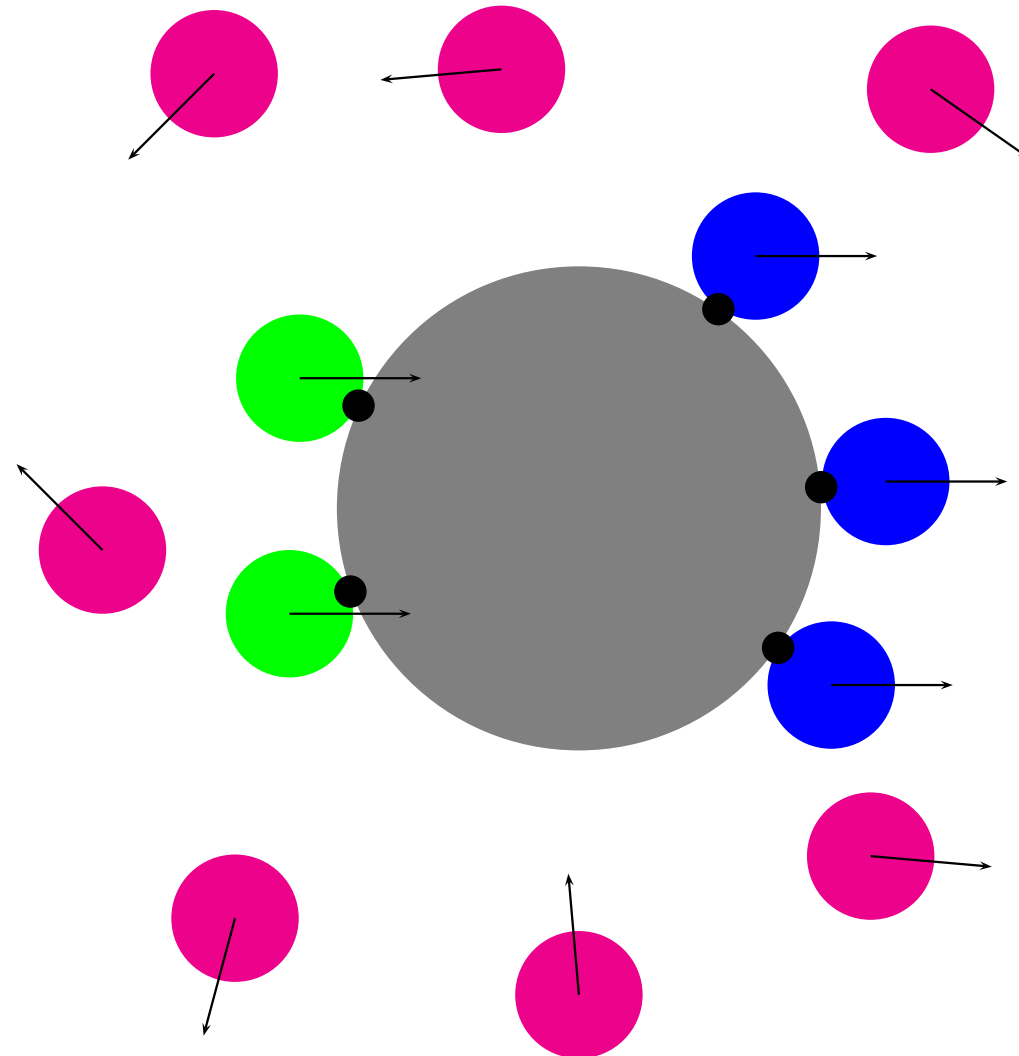
Artificial Successes

Allocation Kinetics

Superficial Matches

New Hopes

Conclusions



Collective Transport

Simplification: Decentralized Boundary Coverage

Overview

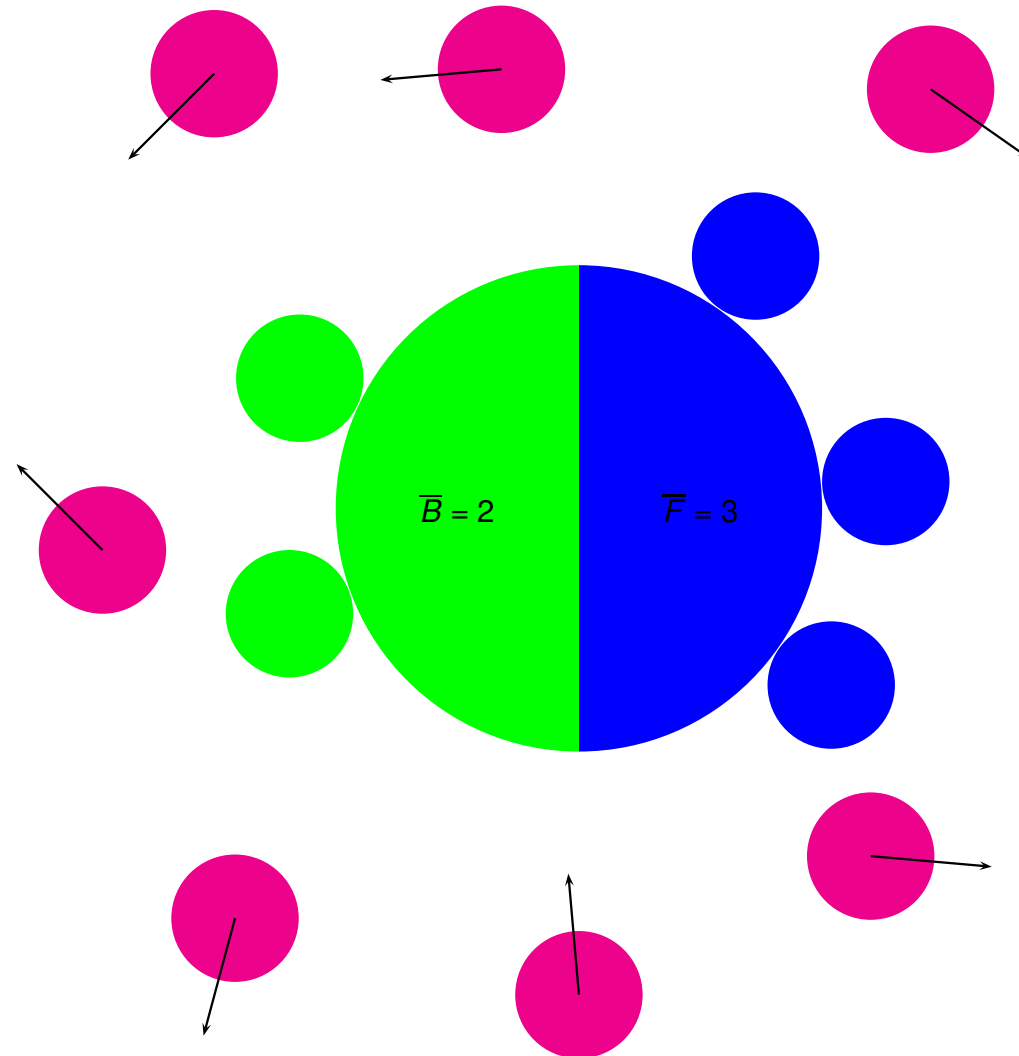
Artificial Successes

Allocation Kinetics

Superficial Matches

New Hopes

Conclusions



Stochastic Boundary Coverage

Physical Inspiration: Langmuir Adsorption

Overview

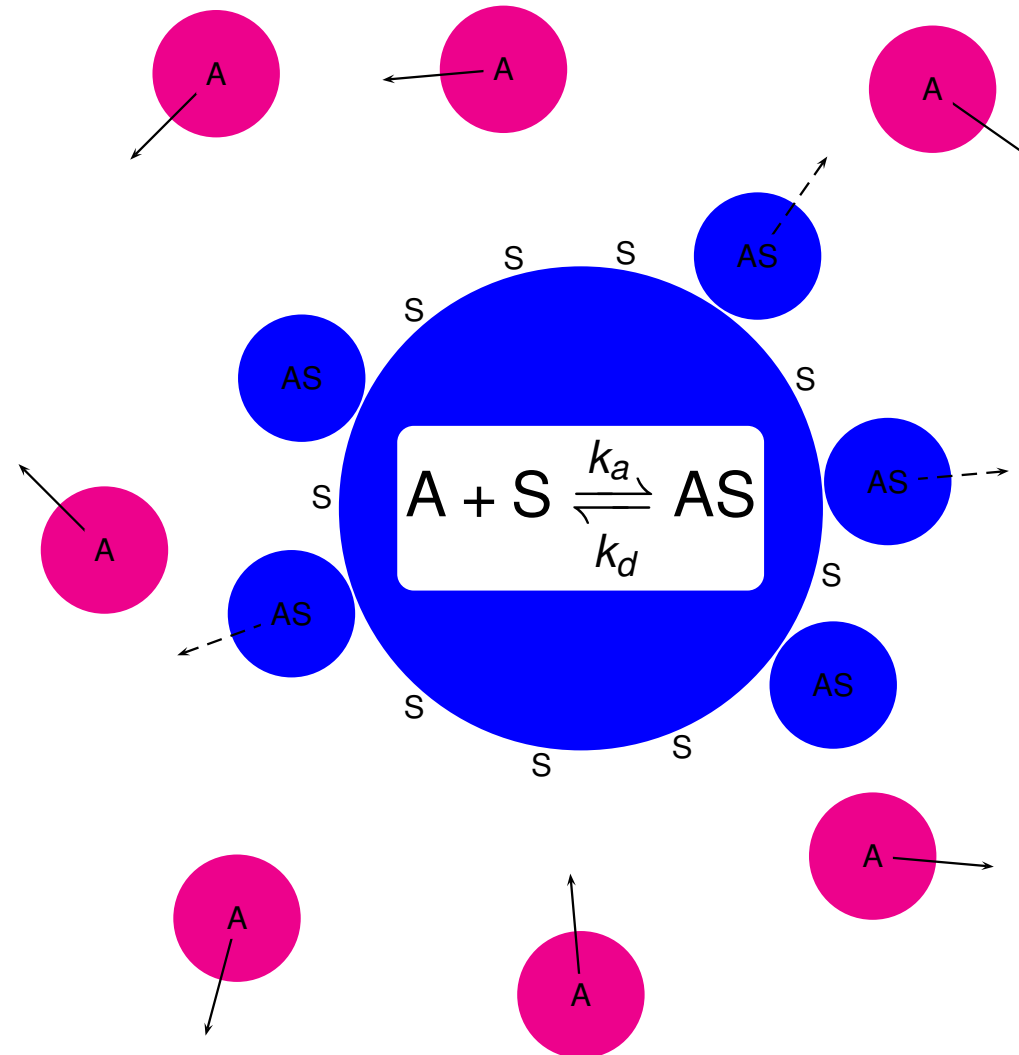
Artificial Successes

Allocation Kinetics

Superficial Matches

New Hopes

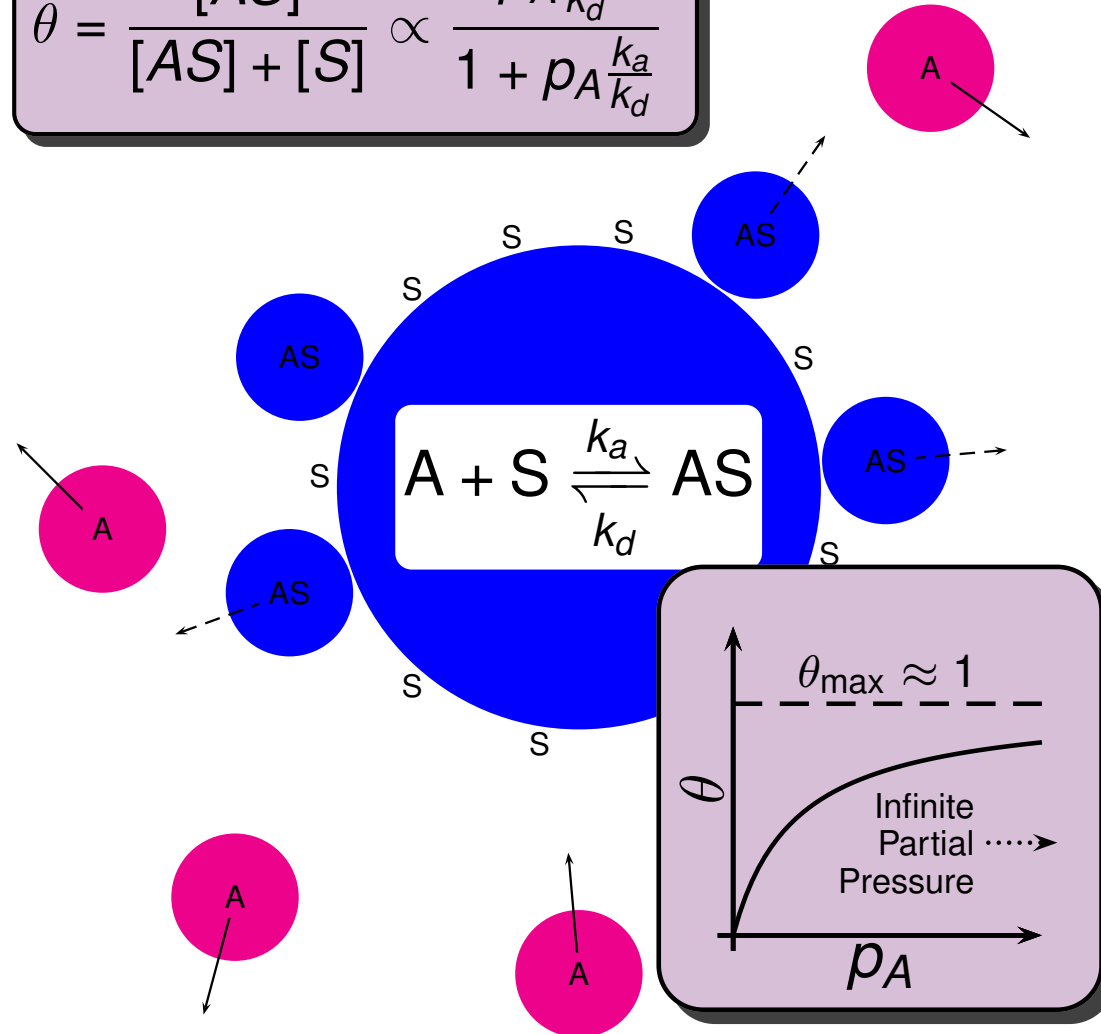
Conclusions



Stochastic Boundary Coverage

Physical Inspiration: Langmuir Adsorption

$$\theta = \frac{[AS]}{[AS] + [S]} \propto \frac{p_A \frac{k_a}{k_d}}{1 + p_A \frac{k_a}{k_d}}$$



Overview

Artificial Successes

Allocation Kinetics

Superficial Matches

New Hopes

Conclusions

Stochastic Boundary Coverage

Design of Robotic Adsorption

Overview

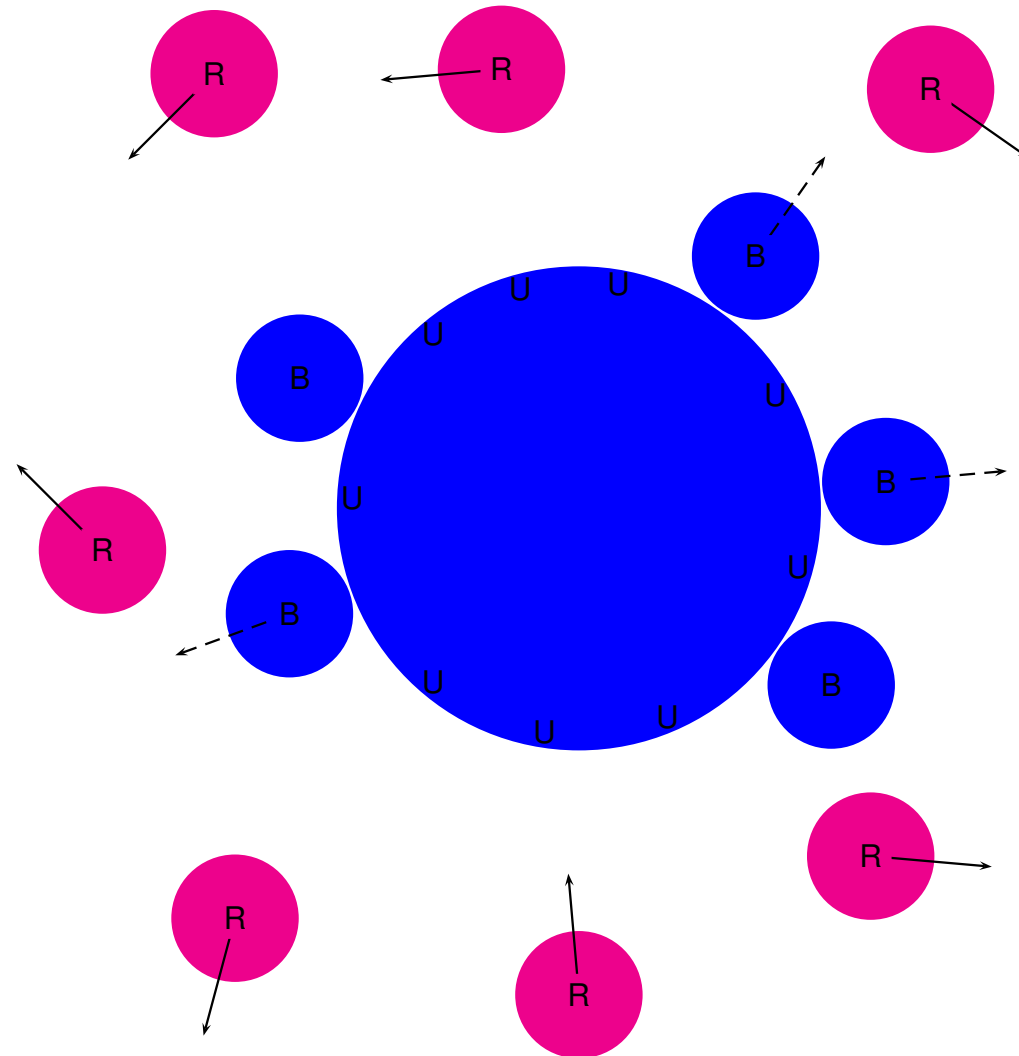
Artificial Successes

Allocation Kinetics

Superficial Matches

New Hopes

Conclusions



Stochastic Boundary Coverage

Design of Robotic Adsorption

Overview

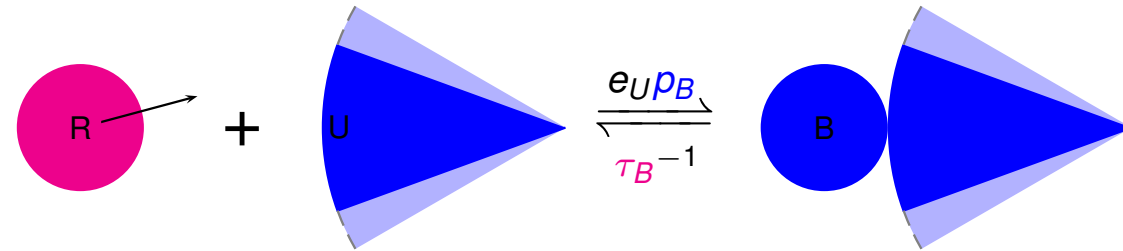
Artificial Successes

Allocation Kinetics

Superficial Matches

New Hopes

Conclusions



$$\frac{[B]}{[U]} = R_0 \frac{e_U p_B}{\tau_B^{-1}}$$

R_0 : free-robot concentration

e_U : robot-load-site encounter rate

p_B : probability of binding

τ_B : mean time before unbinding

- **Control strategy:** Choose probability p_B and time τ_B for desired allocation.

Stochastic Boundary Coverage

Design of Robotic Adsorption

Overview

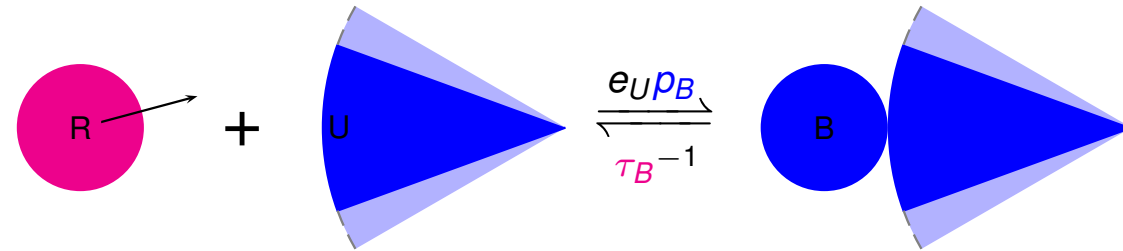
Artificial Successes

Allocation Kinetics

Superficial Matches

New Hopes

Conclusions



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- Choices depend on R_0 . Not scalable.

Stochastic Boundary Coverage

Design of Robotic Adsorption

Overview

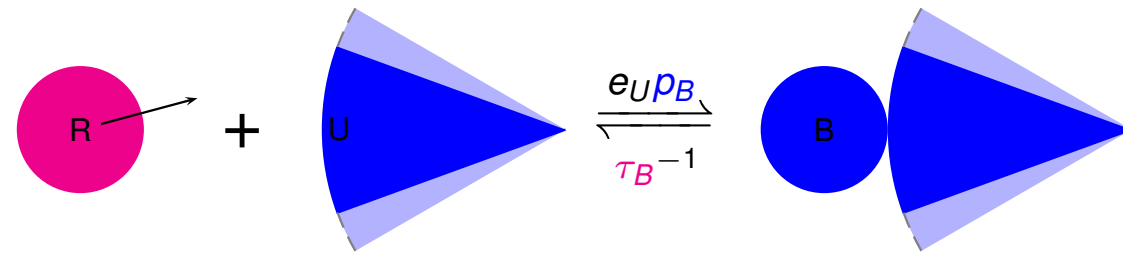
Artificial Successes

Allocation Kinetics

Superficial Matches

New Hopes

Conclusions



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- Choices depend on R_0 . Not scalable.
- Choices depend on e_U . **How to model e_U *ab initio*?**

Stochastic Boundary Coverage

Biochemical Inspiration: Catalyzing Enzymes

Overview

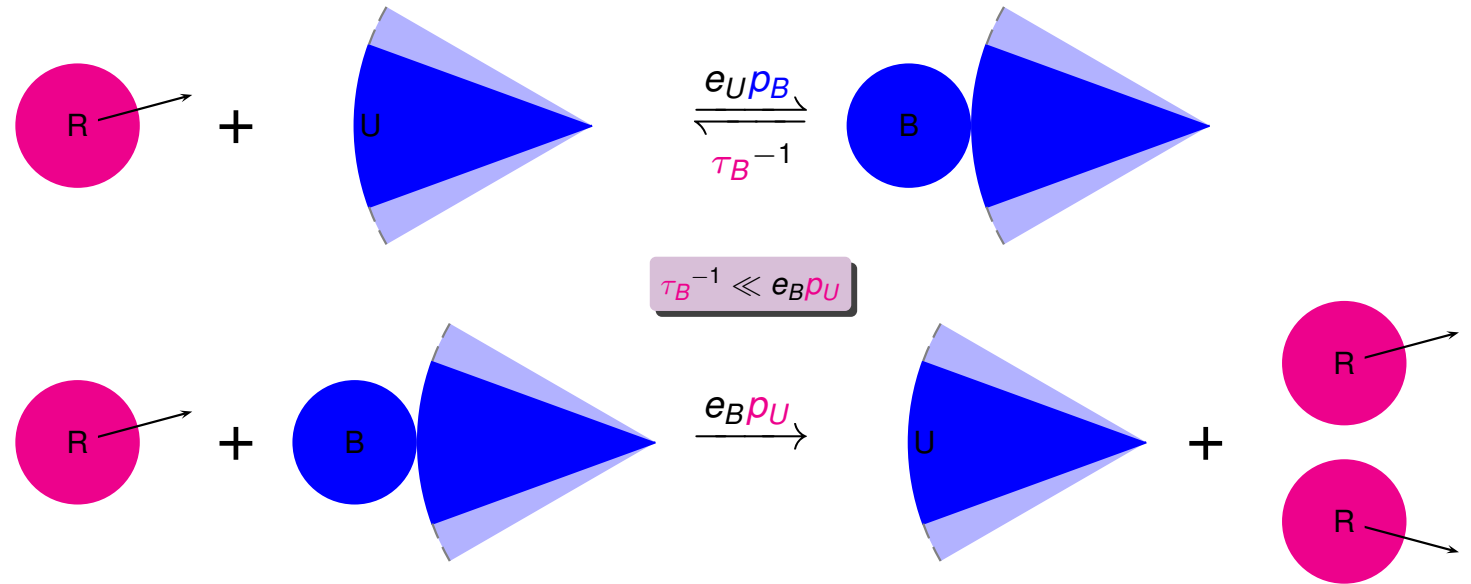
Artificial Successes

Allocation Kinetics

Superficial Matches

New Hopes

Conclusions



Stochastic Boundary Coverage

Catalyzing Robozymes

Overview

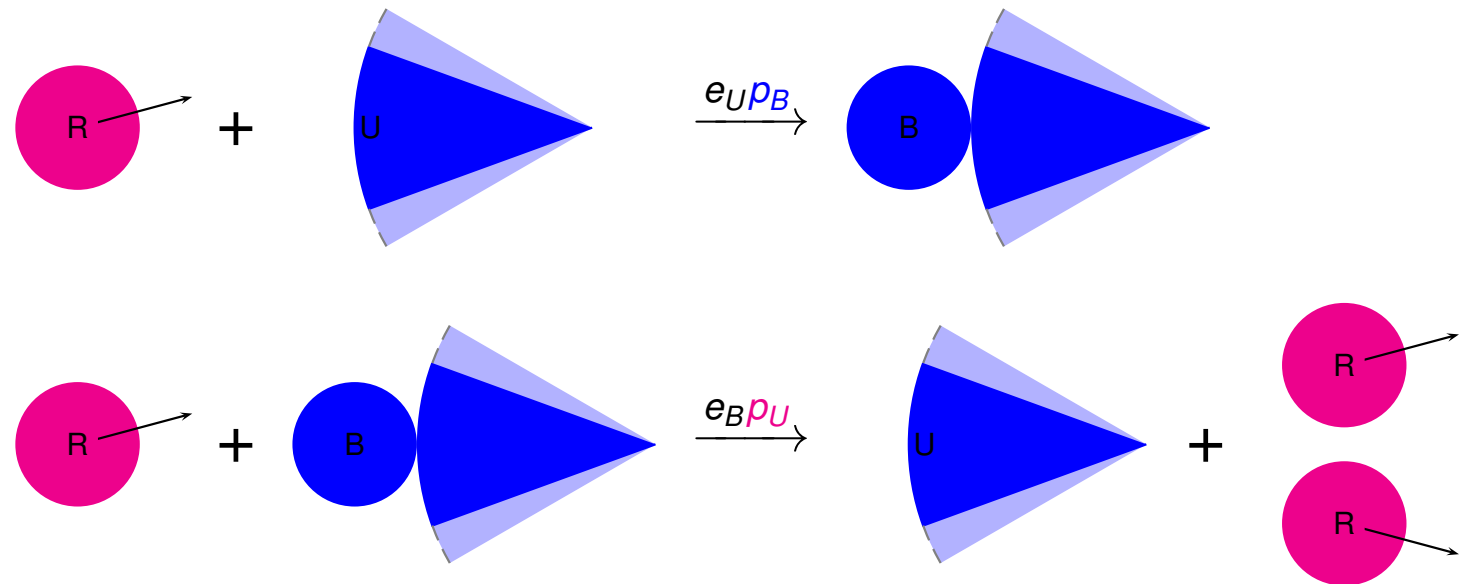
Artificial Successes

Allocation Kinetics

Superficial Matches

New Hopes

Conclusions



$$\frac{[B]}{[U]} = \frac{R_0 e_U p_B}{R_0 e_B p_U} \approx \frac{p_B}{p_U}$$

R_0 : free-robot concentration

e_U : robot-load-site encounter rate

p_B : probability of binding

e_B : robot-bound-complex encounter rate

p_U : probability of unbinding

- **Control strategy:** Choose probabilities p_B and p_U for desired allocation.

Stochastic Boundary Coverage

Catalyzing Robozymes

Overview

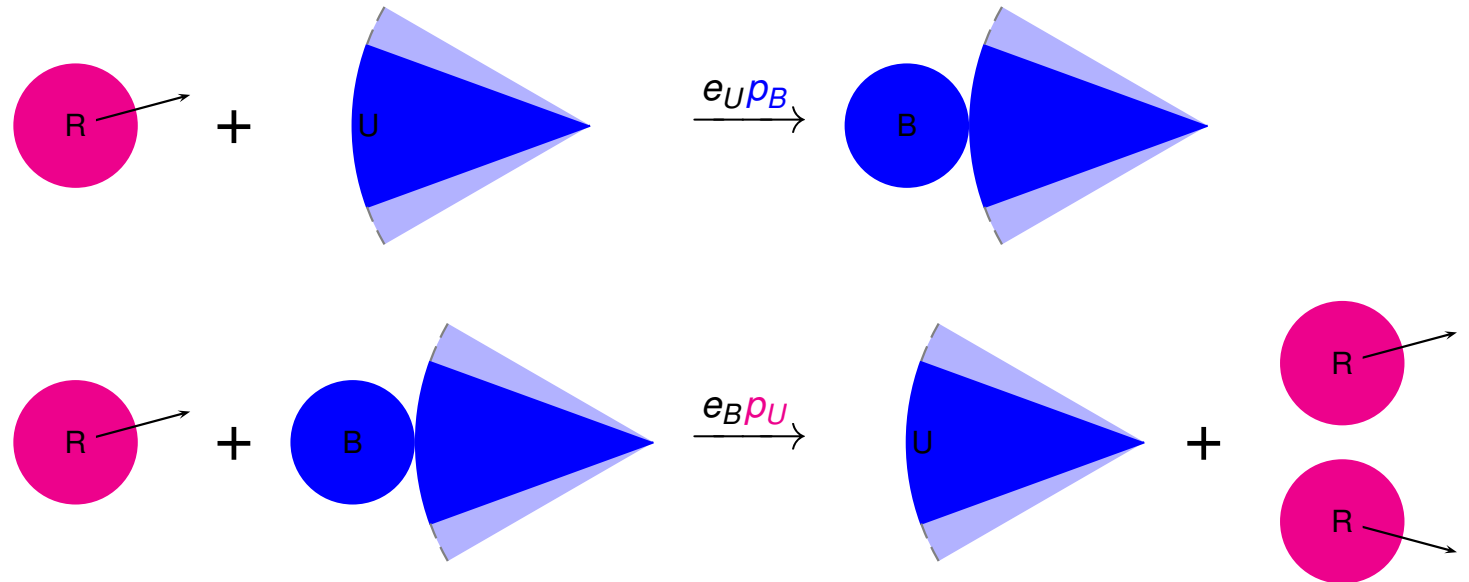
Artificial Successes

Allocation Kinetics

Superficial Matches

New Hopes

Conclusions



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- Scalable.

Stochastic Boundary Coverage

Catalyzing Robozymes

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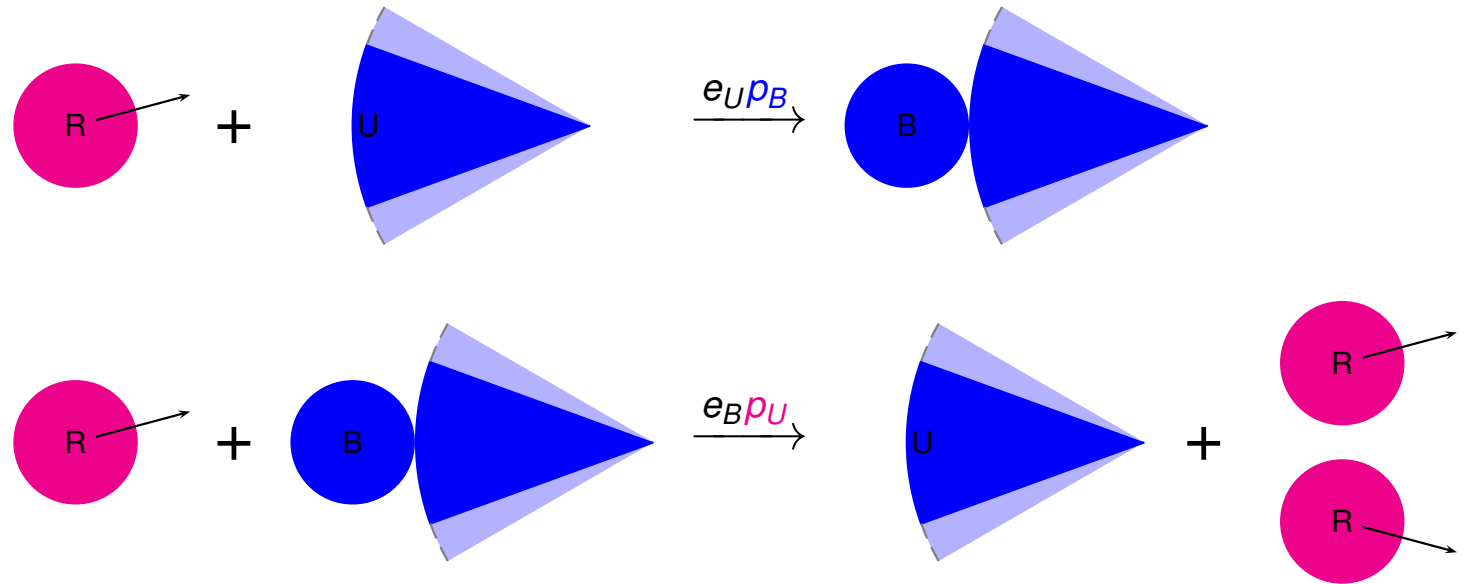
Artificial Successes

Allocation Kinetics

Superficial Matches

New Hopes

Conclusions



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p_U : probability of unbinding

- **Control strategy:** Choose probabilities p_B and p_U for desired allocation.
- Scalable.
- Choices depend on $e_U/e_B = \text{constant} \approx 1$, which has geometric derivation.

Stochastic Boundary Coverage

Derivation of Saturation Occupancy

Overview

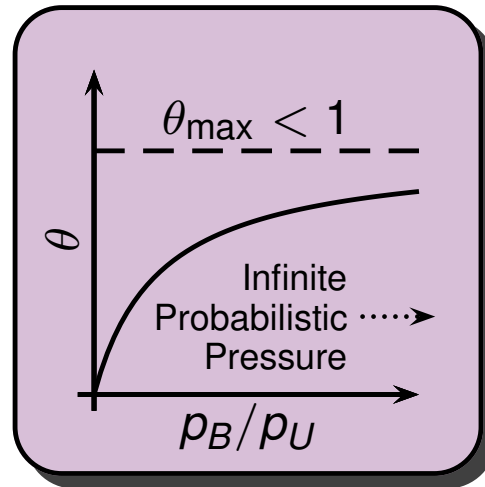
Artificial Successes

Allocation Kinetics

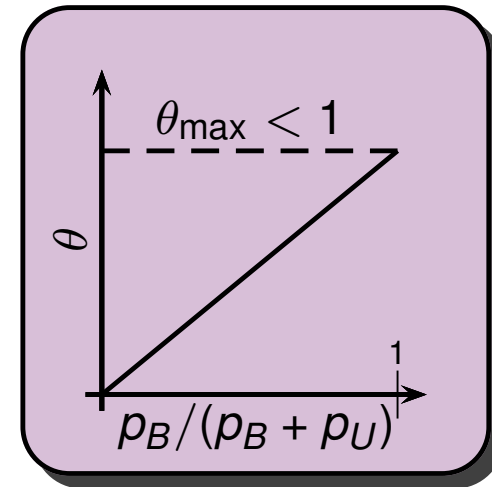
Superficial Matches

New Hopes

Conclusions



sensu Langmuir



Design case?

Stochastic Boundary Coverage

Derivation of Saturation Occupancy

Overview

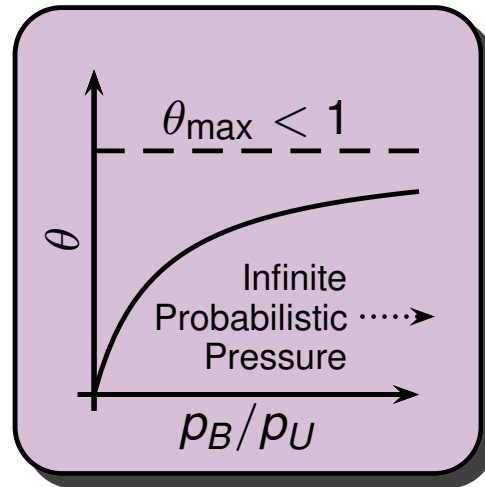
Artificial Successes

Allocation Kinetics

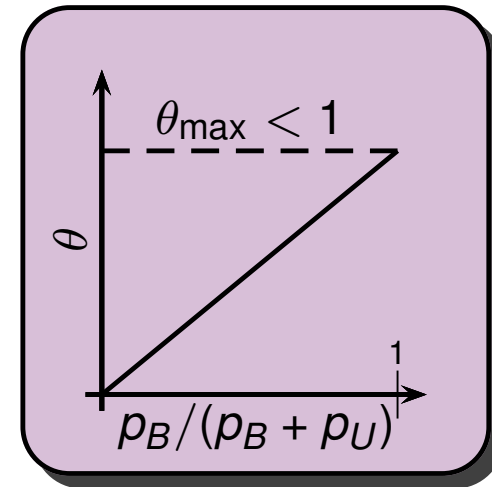
Superficial Matches

New Hopes

Conclusions



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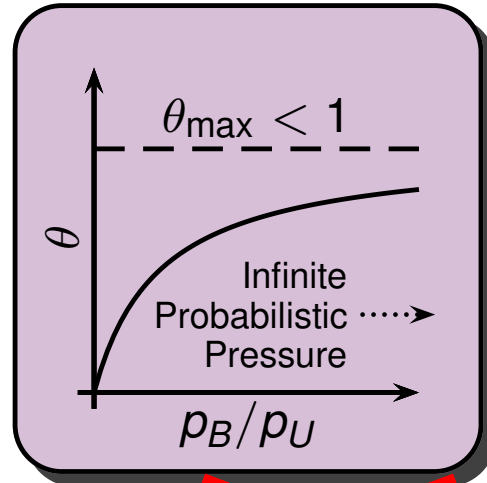
Design case?

$$\theta_{\max} \stackrel{?!}{=} 0.75$$

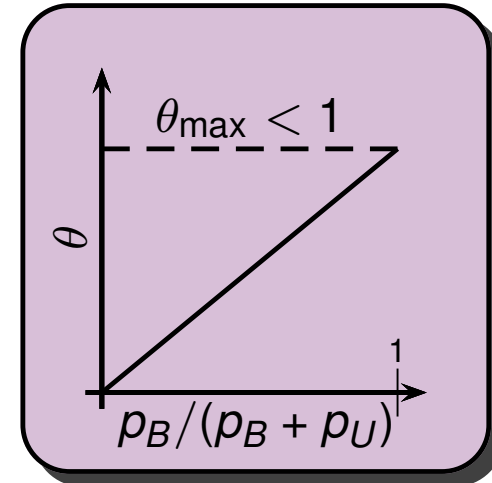
Stochastic Boundary Coverage

Rényi's Parking Problem Revisited

- Overview
- Artificial Successes
- Allocation Kinetics
- Superficial Matches
- New Hopes
- Conclusions



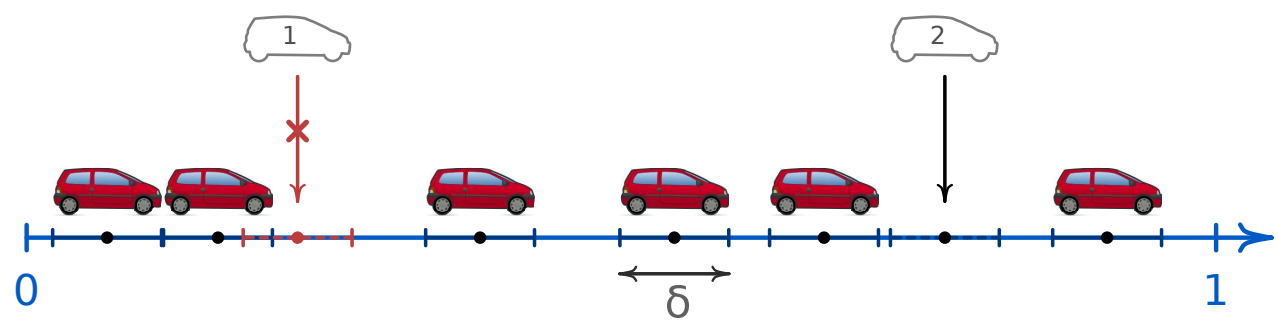
~~sensu Langmuir~~



Design case?



$$\theta_{\max} = 0.74759792025341143517 \dots$$



Stochastic Boundary Coverage

Rényi's Parking Problem Revisited

Overview

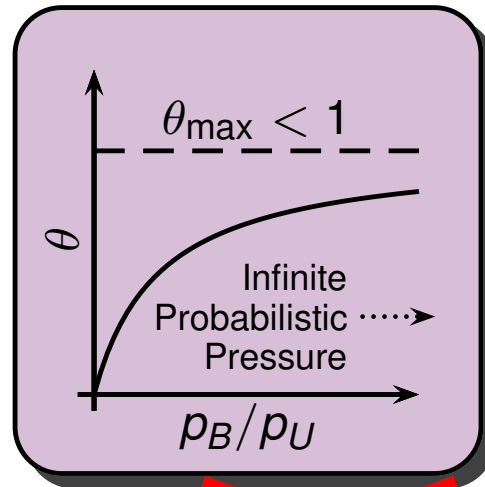
Artificial Successes

Allocation Kinetics

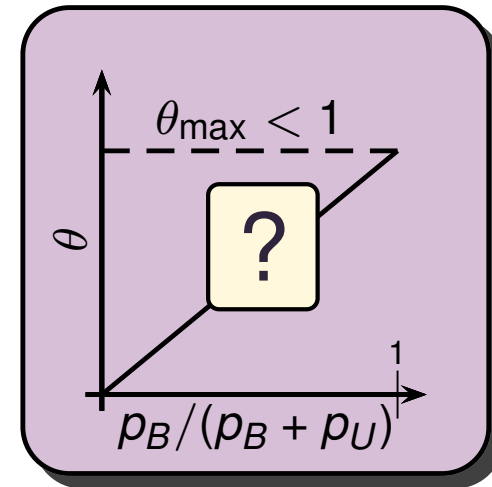
Superficial Matches

New Hopes

Conclusions



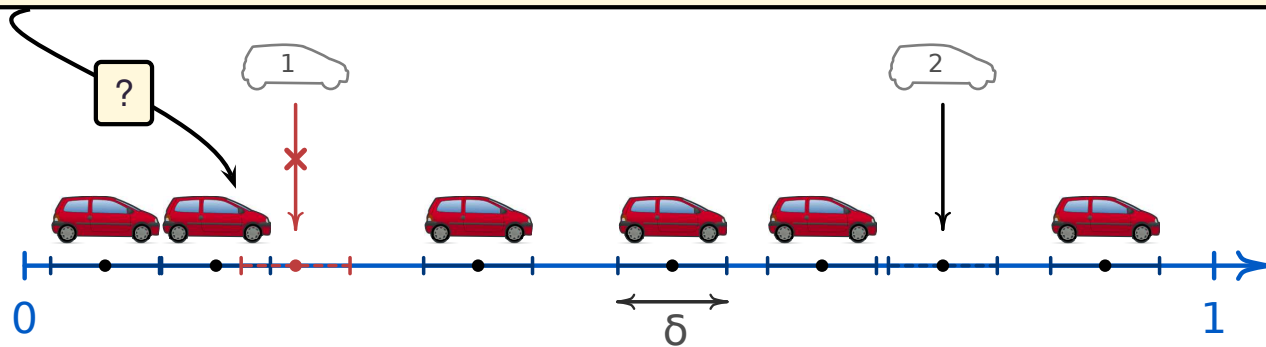
~~sensu Langmuir~~



Design case?

Rényi!

What about when encountered cars sometimes leave?



Stochastic Boundary Coverage

Random Sequential Attachment with Detachment (Pavlic et al. 2014)

Overview

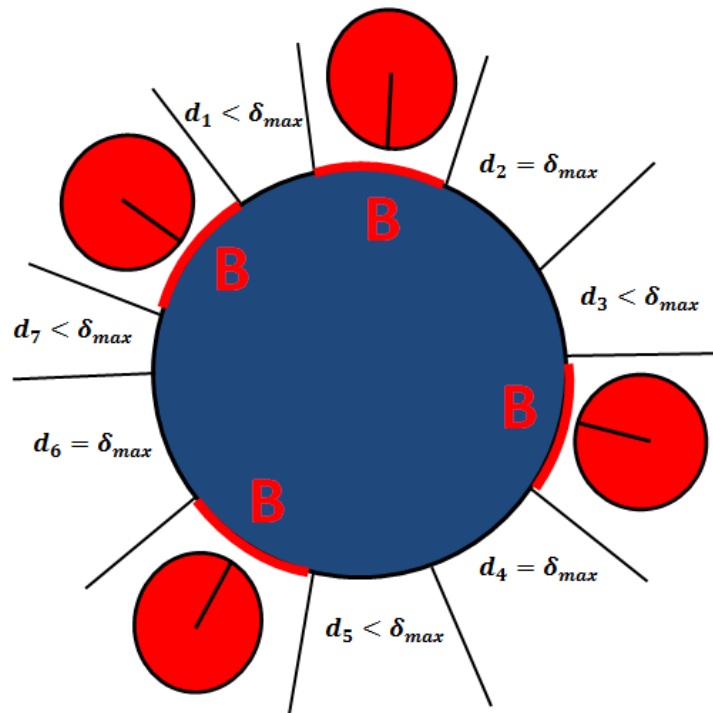
Artificial Successes

Allocation Kinetics

Superficial Matches

New Hopes

Conclusions



Spatial correction

$$\frac{1 + \delta}{1 + \delta \frac{[B]}{[U]}} \frac{[B]}{[U]} = \frac{e_u p_b}{e_b p_u}$$

δ : Mean length of free parking space at equilibrium

Stochastic Boundary Coverage

Random Sequential Attachment with Detachment (Pavlic et al. 2014)

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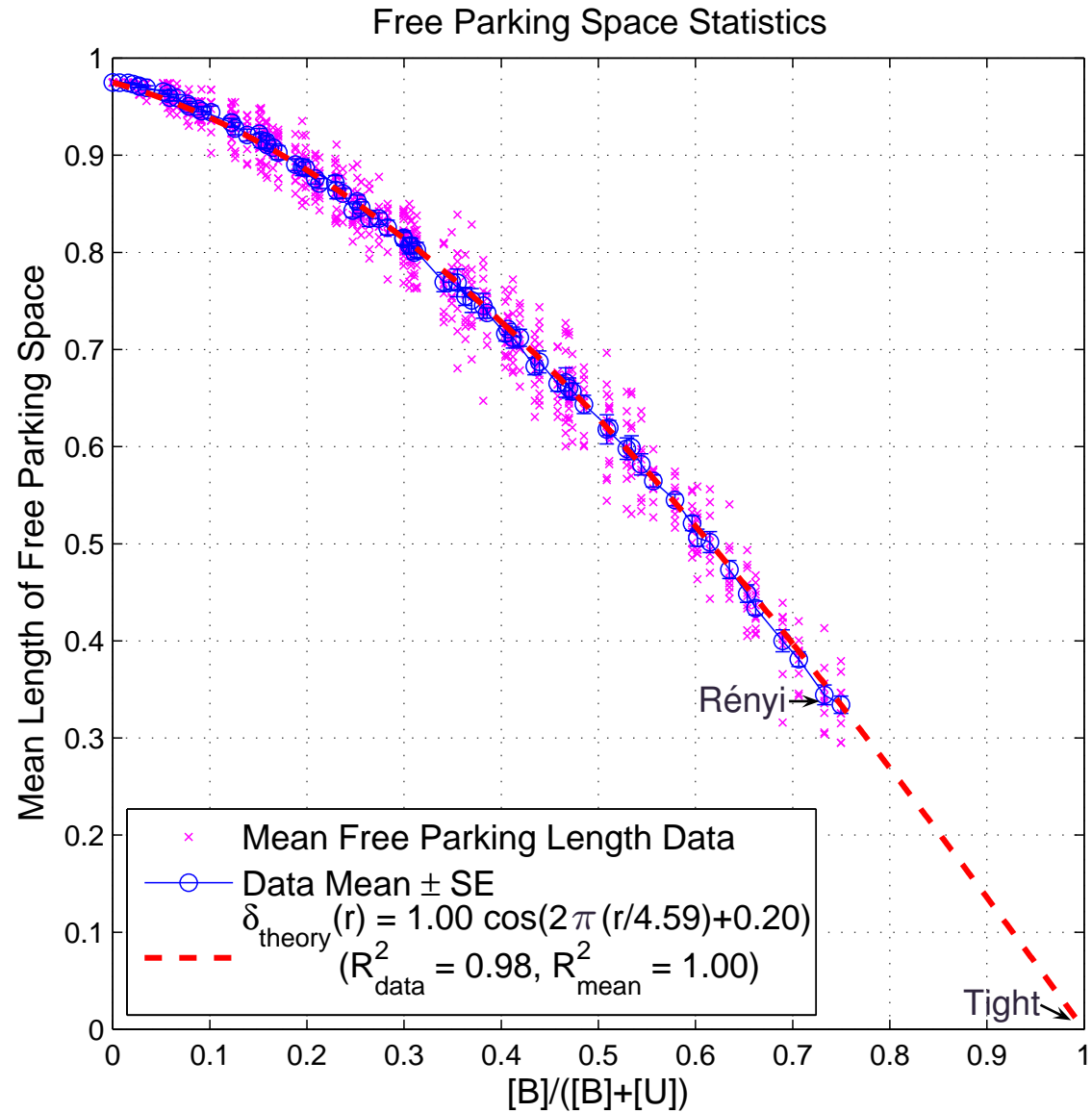
Artificial Successes

Allocation Kinetics

Superficial Matches

New Hopes

Conclusions



Stochastic Boundary Coverage

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Overview

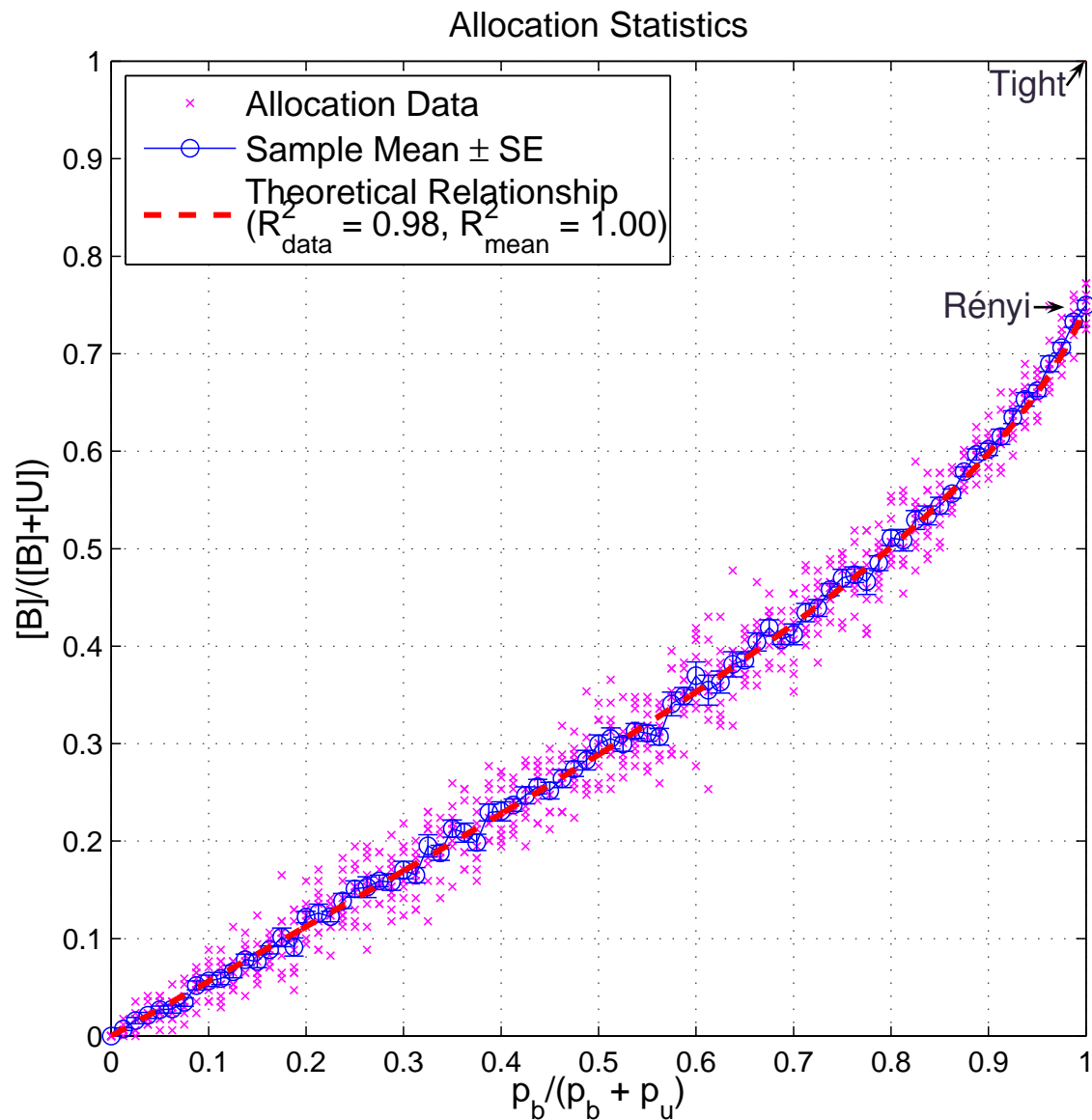
Artificial Successes

Allocation Kinetics

Superficial Matches

New Hopes

Conclusions



Stochastic Boundary Coverage

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Overview

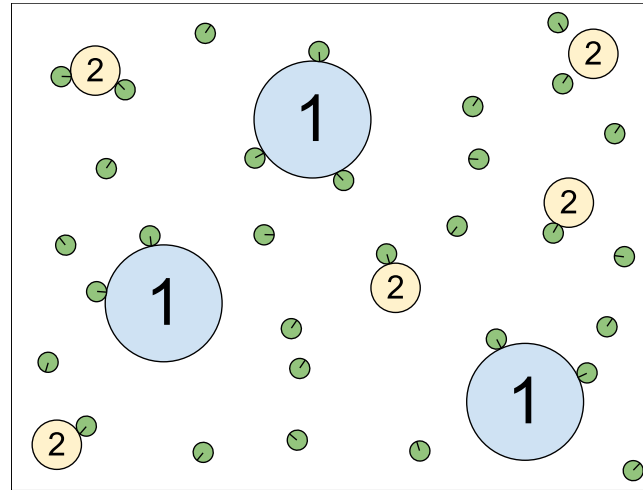
Artificial Successes

Allocation Kinetics

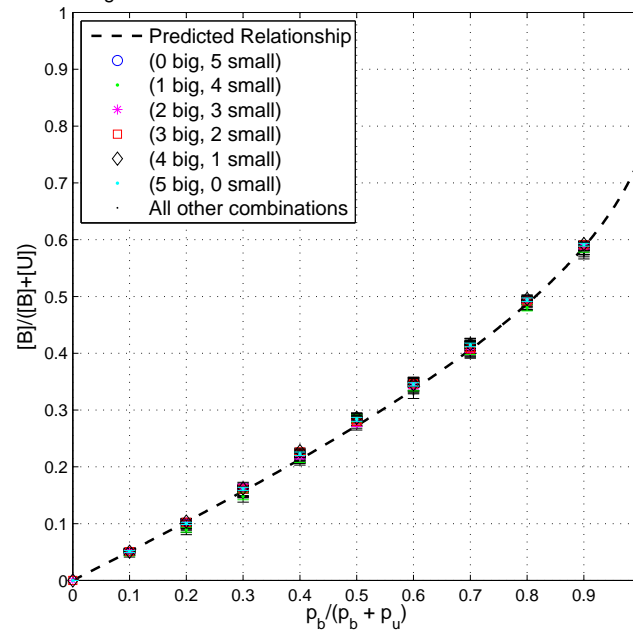
Superficial Matches

New Hopes

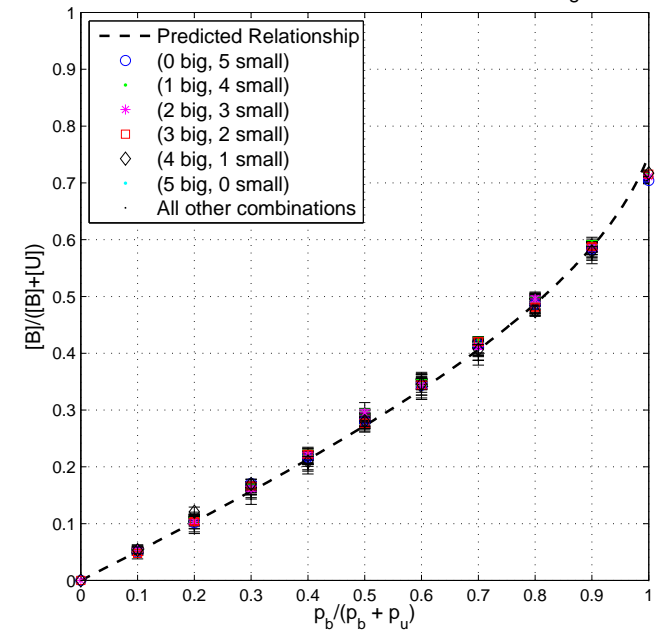
Conclusions



Big-Disk Allocation Statistics in the Presence of Small Disks



Small-Disk Allocation Statistics in the Presence of Big Disks



Stochastic Boundary Coverage

Random Sequential Attachment with Detachment (Pavlic et al. 2013)

Overview

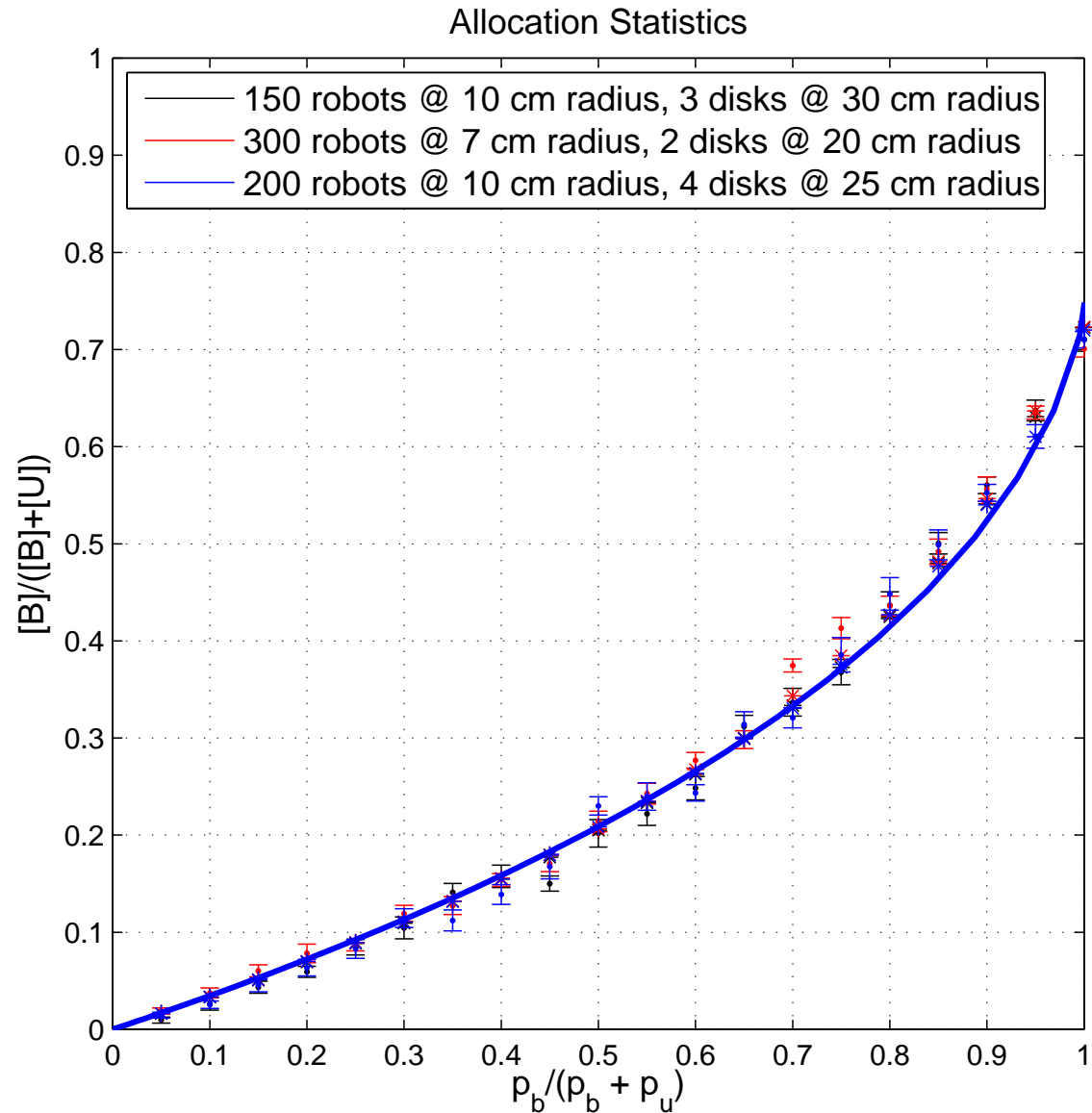
Artificial Successes

Allocation Kinetics

Superficial Matches

New Hopes

Conclusions



Stochastic Boundary Coverage

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Overview

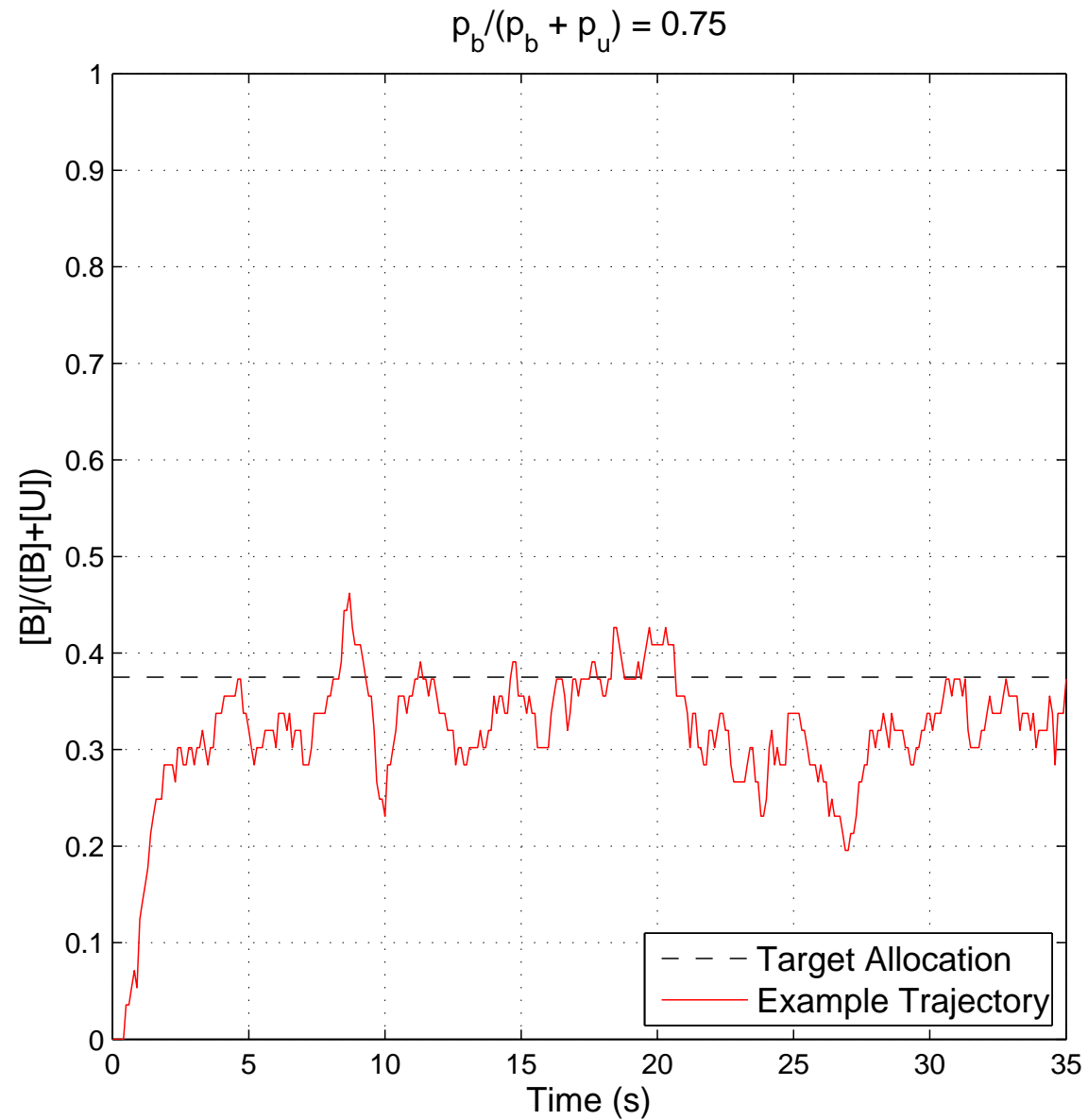
Artificial Successes

Allocation Kinetics

Superficial Matches

New Hopes

Conclusions



Stochastic Boundary Coverage

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Overview

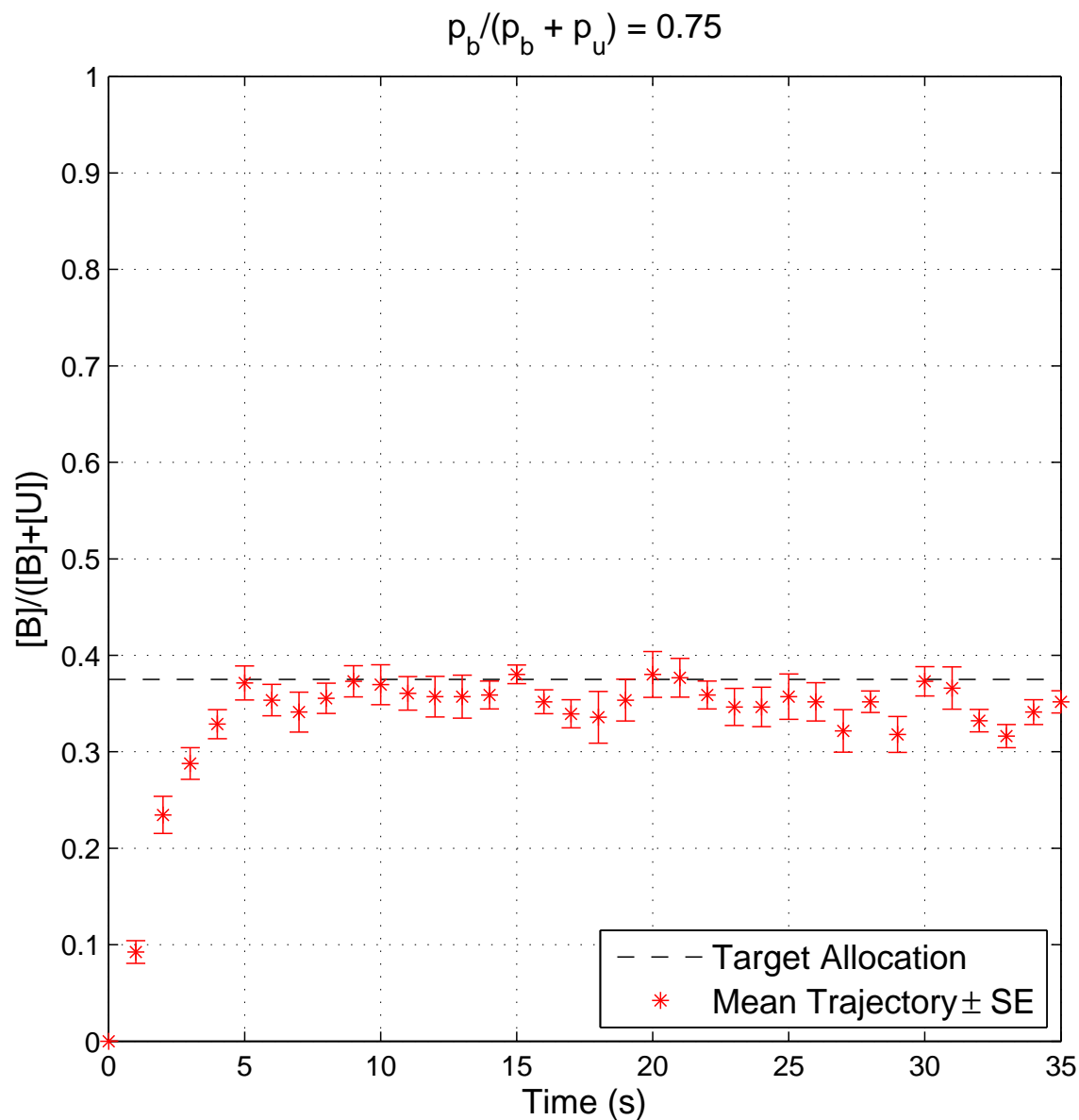
Artificial Successes

Allocation Kinetics

Superficial Matches

New Hopes

Conclusions



Stochastic Boundary Coverage

Random Sequential Attachment with Detachment (Pavlic et al. 2014)

Overview

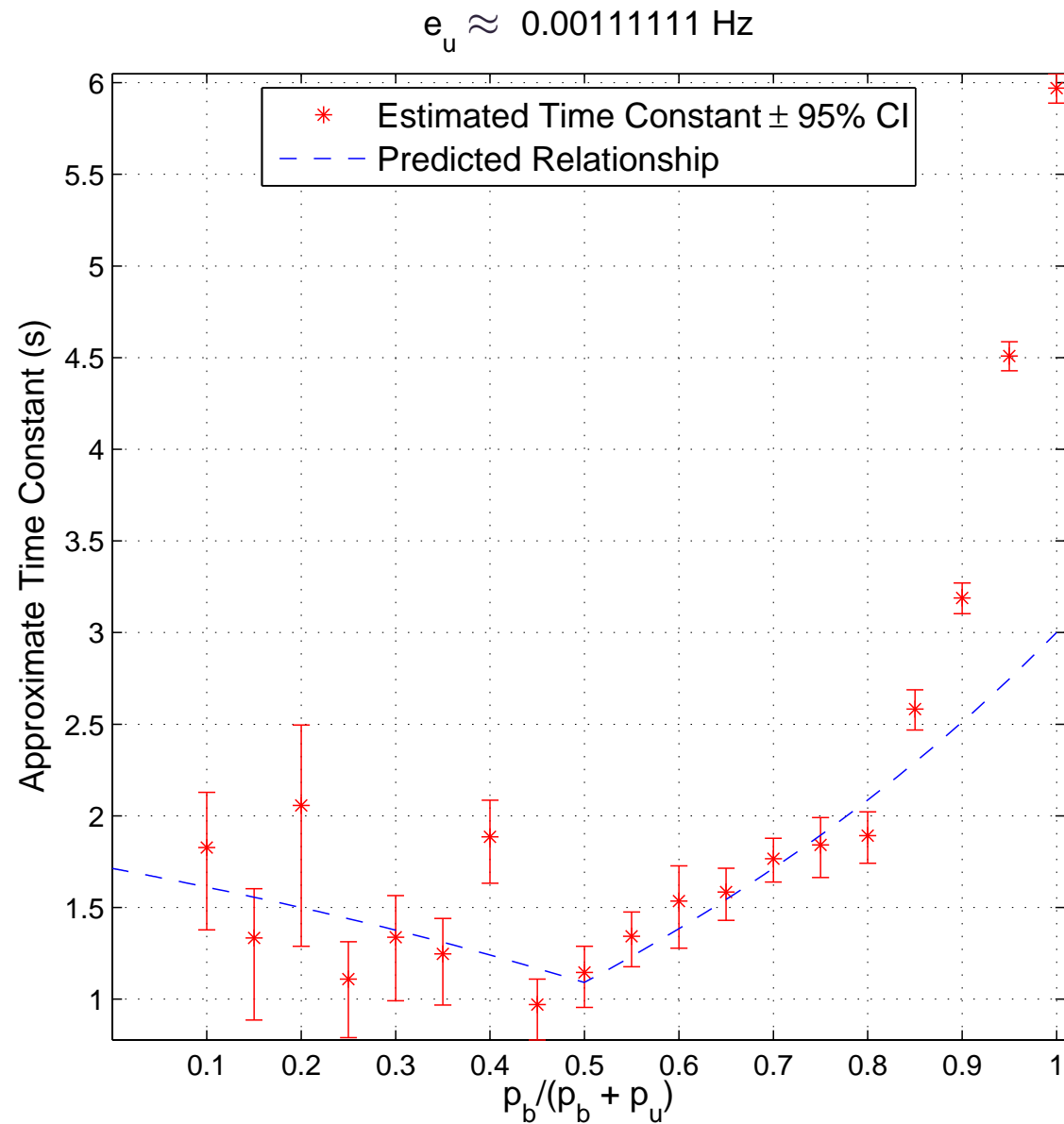
Artificial Successes

Allocation Kinetics

Superficial Matches

New Hopes

Conclusions



Collective Transport

Decentralized Organization of Teams Carrying Loads

Overview

Artificial Successes

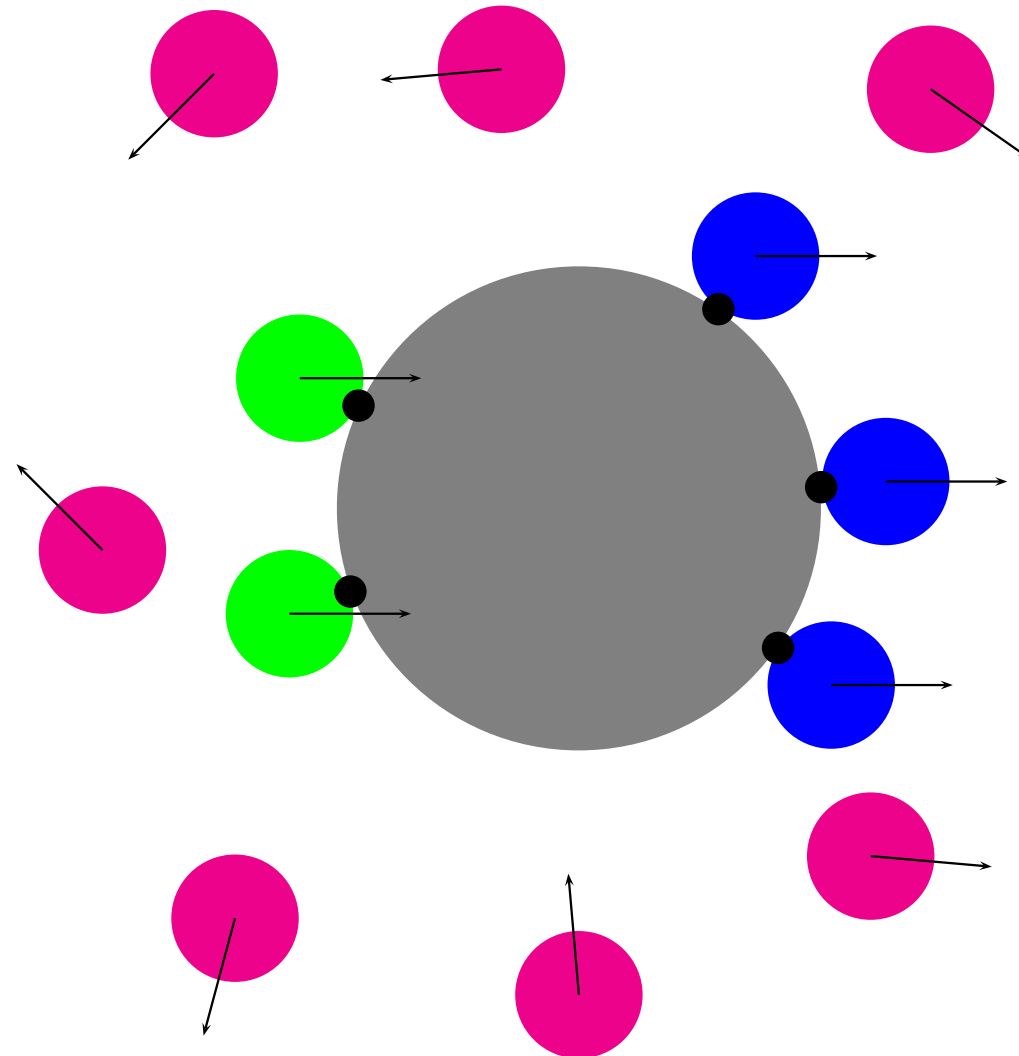
Superficial Matches

Collective Transport

Swarm Assembly

New Hopes

Conclusions



Collective Transport

(Wilson et al. 2014)

Overview

Artificial Successes

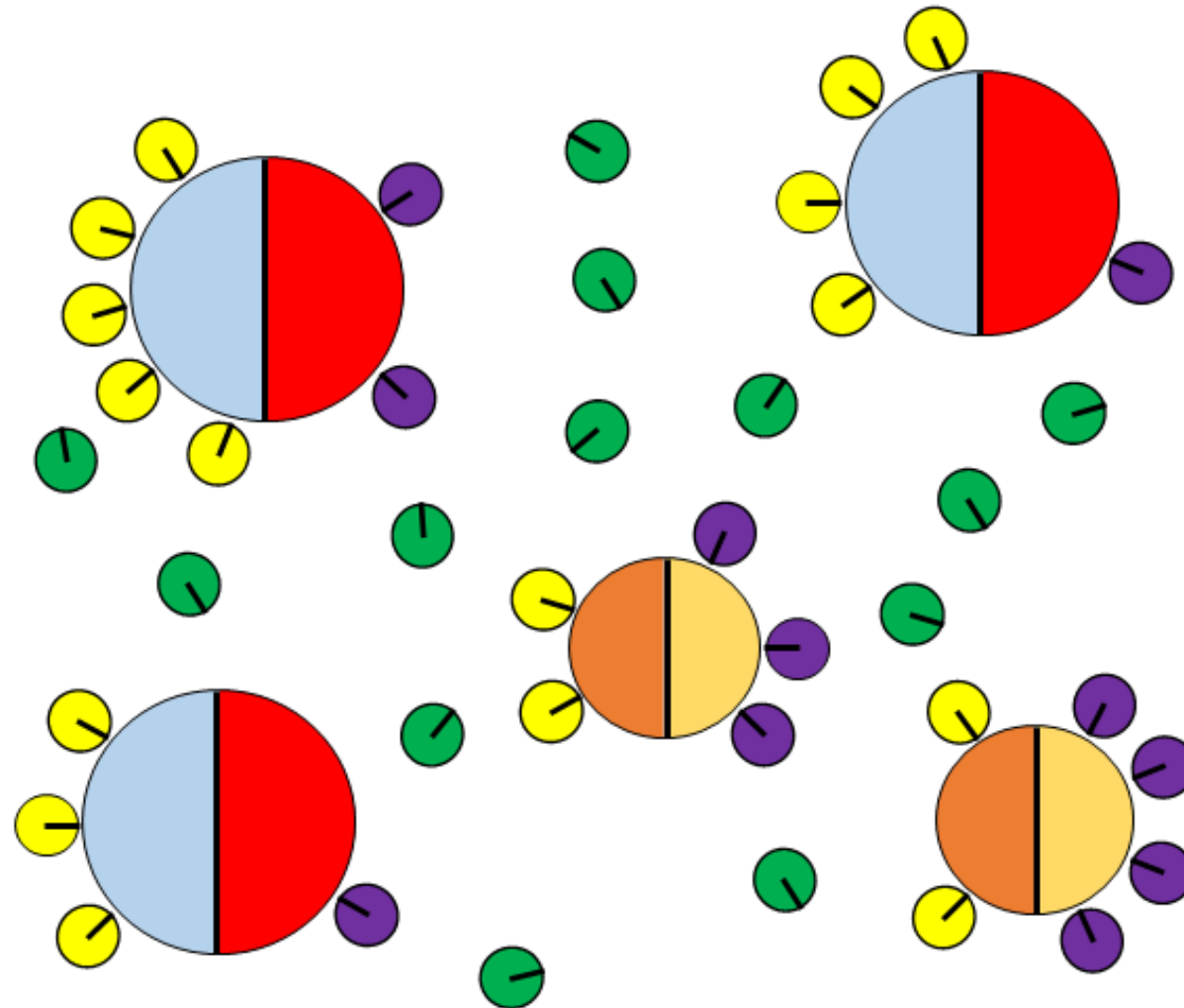
Superficial Matches

Collective Transport

Swarm Assembly

New Hopes

Conclusions



Collective Transport

(Wilson et al. 2014)

Overview

Artificial Successes

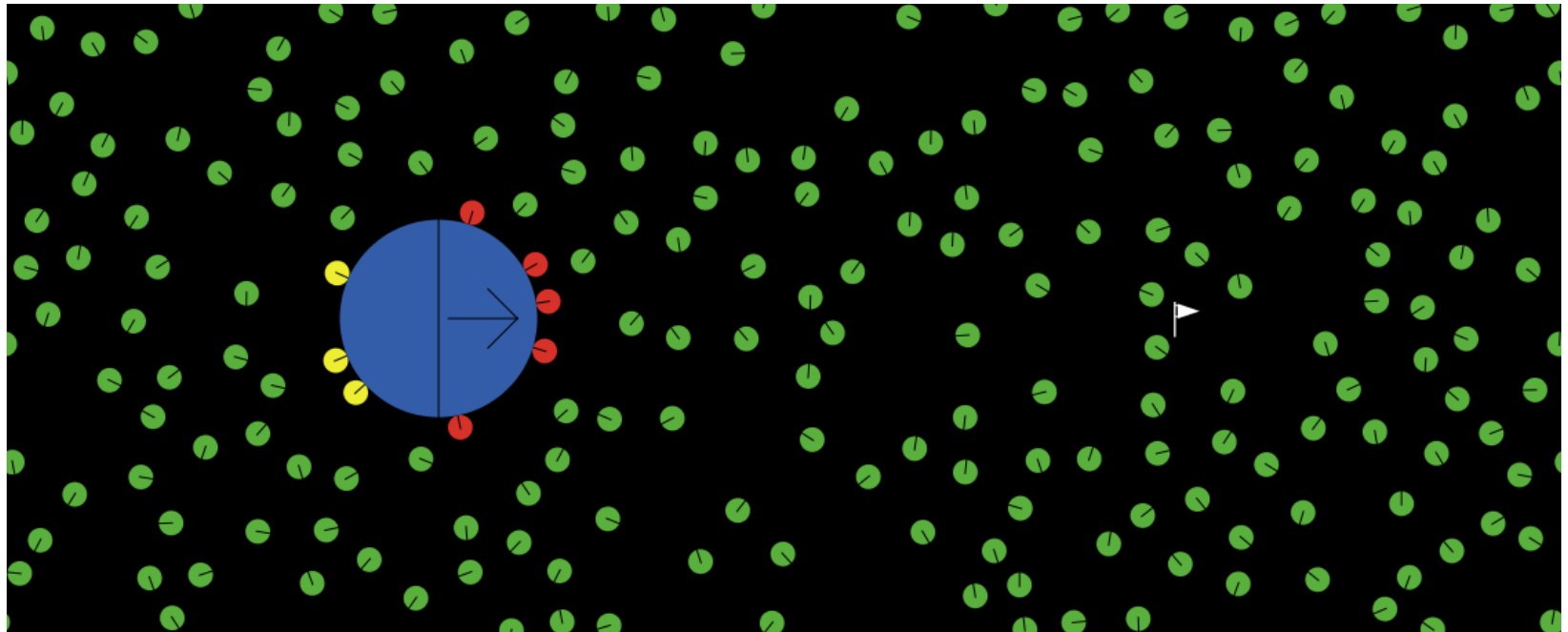
Superficial Matches

Collective Transport

Swarm Assembly

New Hopes

Conclusions



Collective Transport

(Kumar et al. 2013)

Overview

Artificial Successes

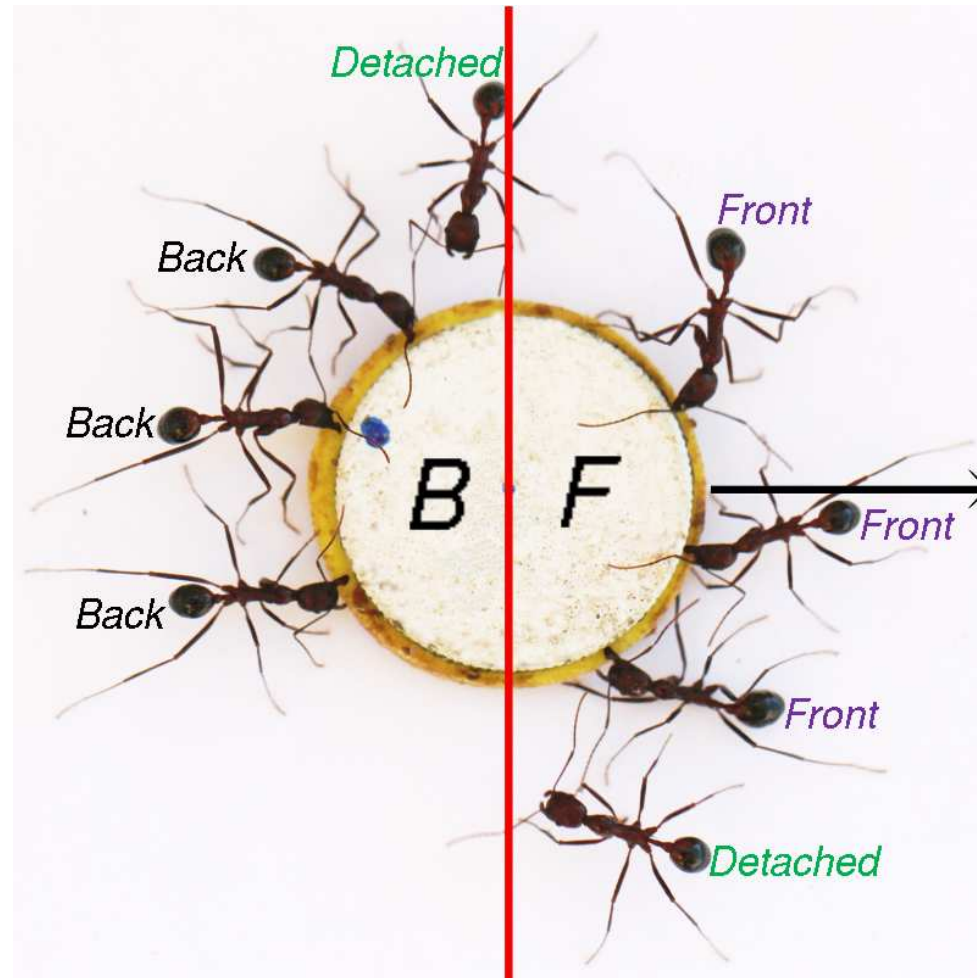
Superficial Matches

Collective Transport

Swarm Assembly

New Hopes

Conclusions



Collective Transport

(Kumar et al. 2013)

Overview

Artificial Successes

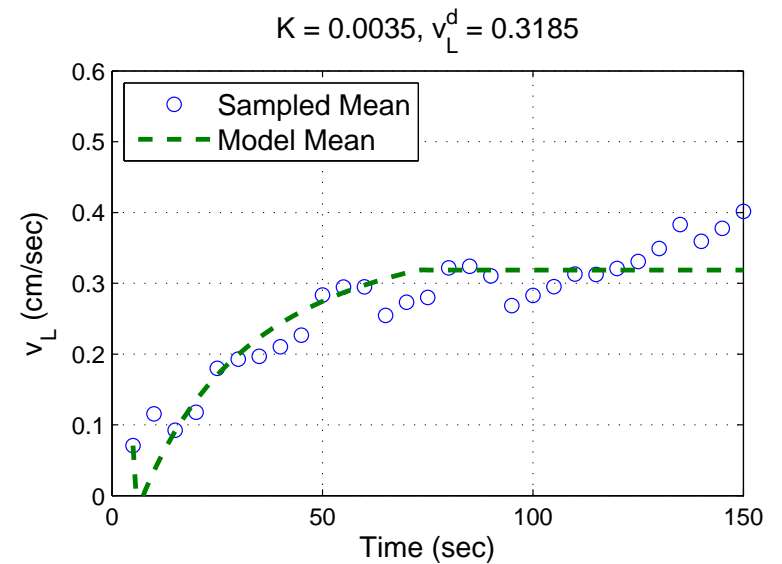
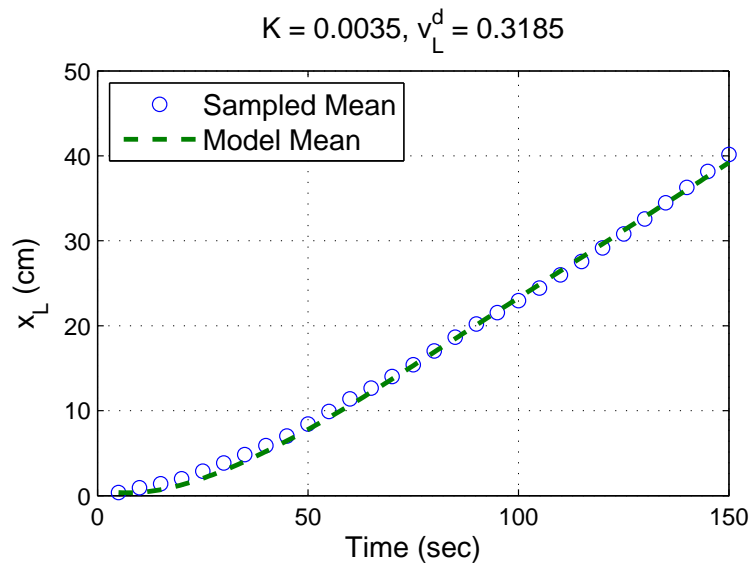
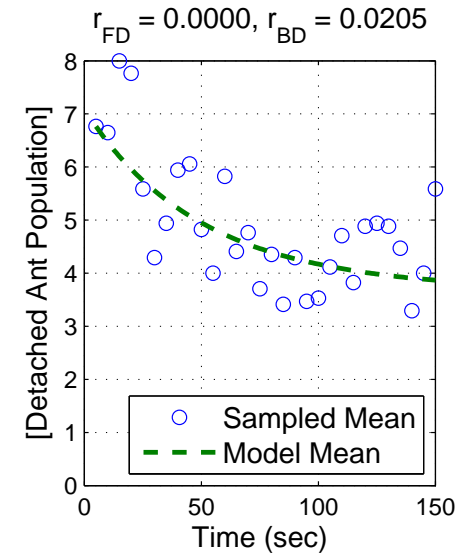
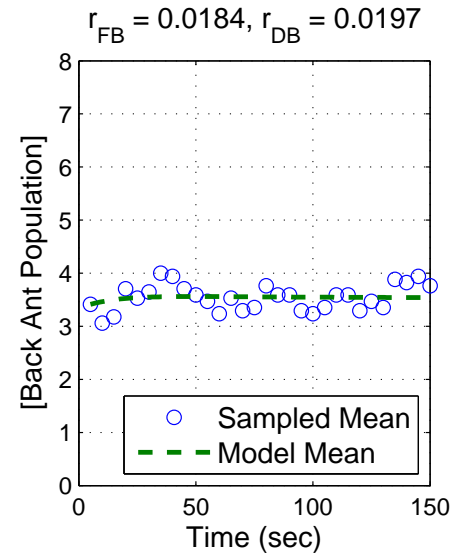
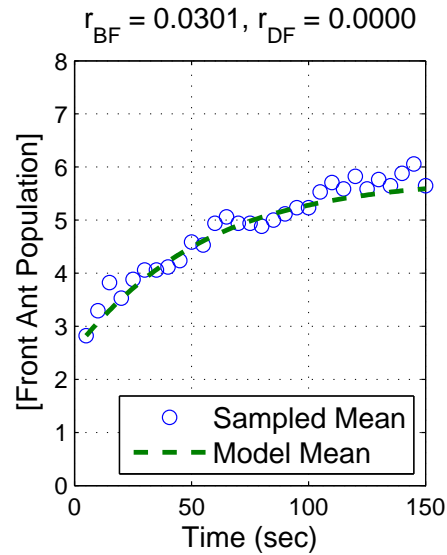
Superficial Matches

Collective Transport

Swarm Assembly

New Hopes

Conclusions



Collective Transport

(Wilson et al. 2014)

Overview

Artificial Successes

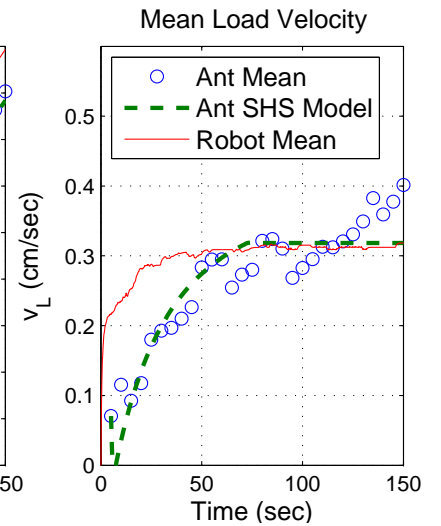
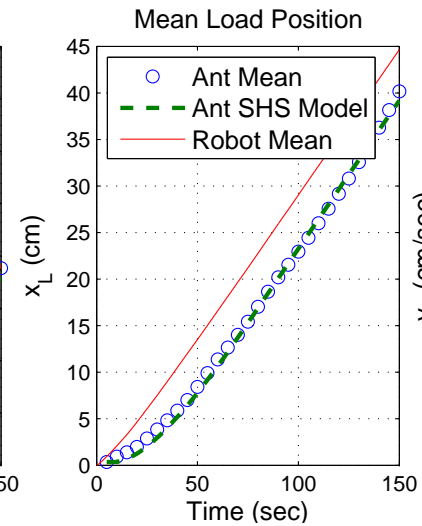
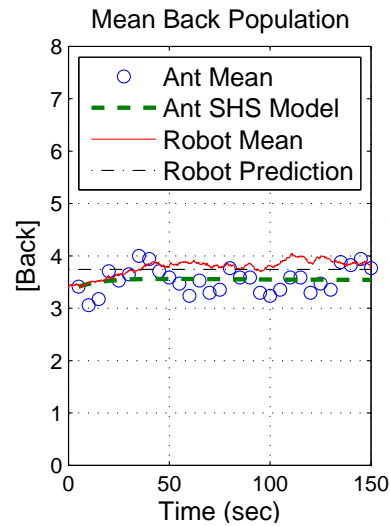
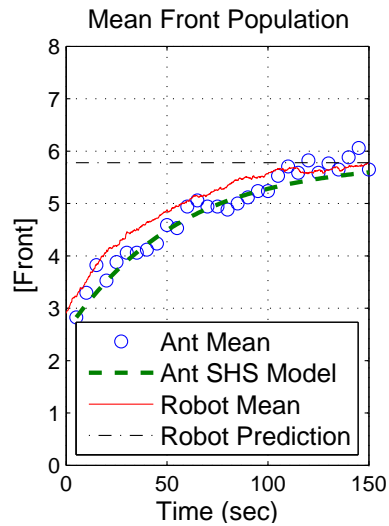
Superficial Matches

Collective Transport

Swarm Assembly

New Hopes

Conclusions



Collective Transport

Decentralized Organization of *Ant* Teams Carrying Loads

Overview

Artificial Successes

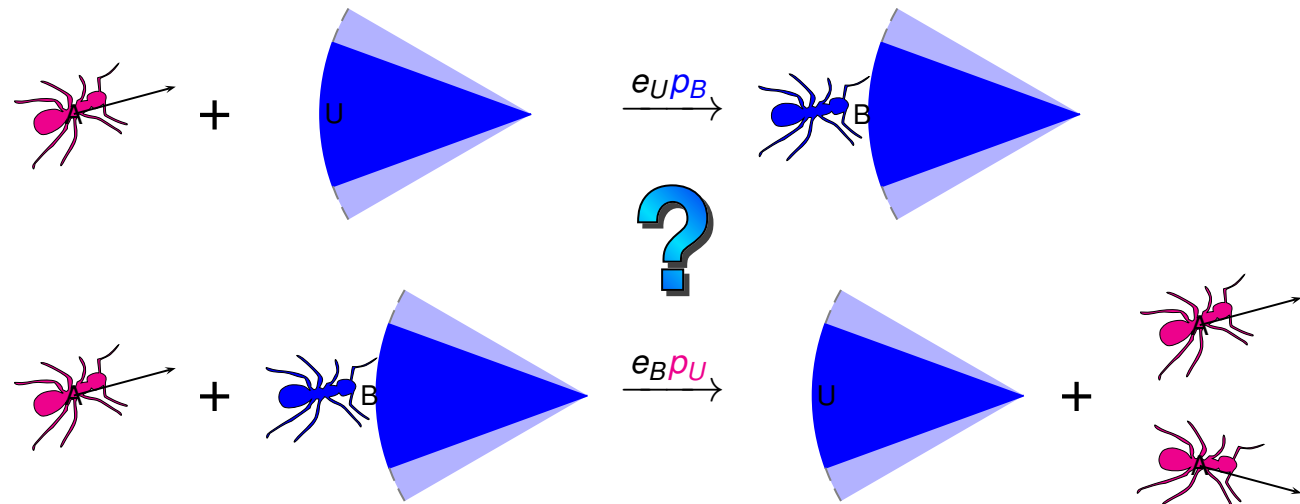
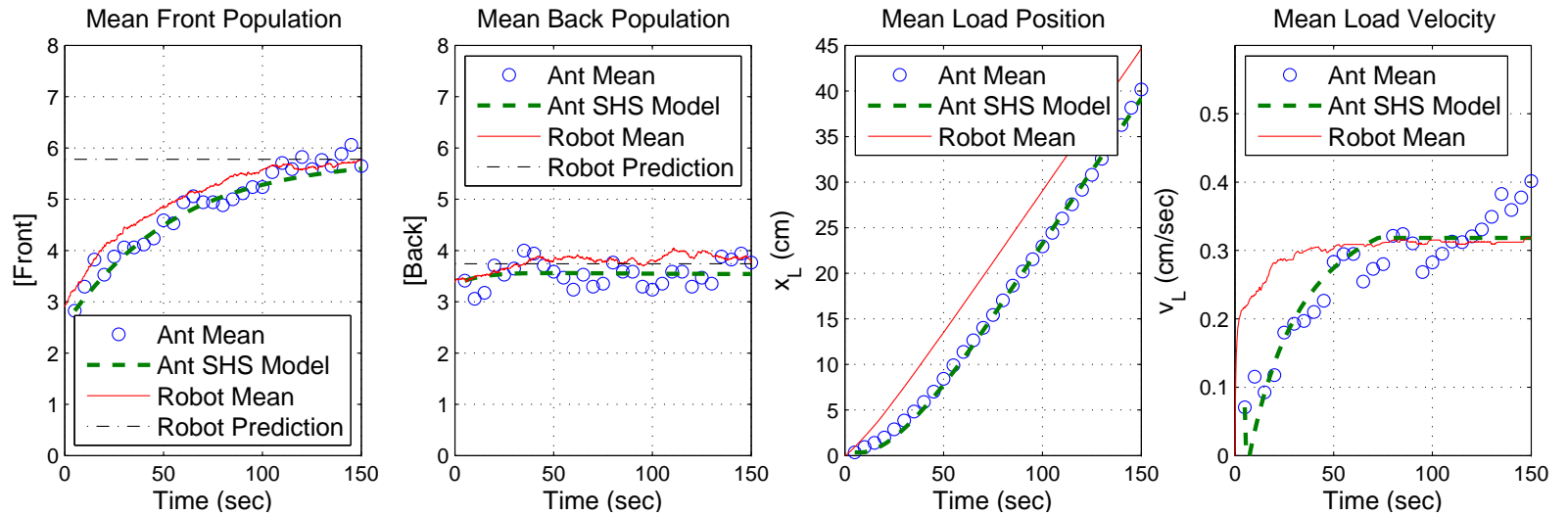
Superficial Matches

Collective Transport

Swarm Assembly

New Hopes

Conclusions



Collective Transport

Decentralized Organization of *Ant* Teams Carrying Loads

Overview

Artificial Successes

Superficial Matches

Collective Transport

Swarm Assembly

New Hopes

Conclusions



Collective Transport

Decentralized Organization of *Ant* Teams Carrying Loads

Overview

Artificial Successes

Superficial Matches

Collective Transport

Swarm Assembly

New Hopes

Conclusions



Collective Transport

Decentralized Organization of *Ant* Teams Carrying Loads

Overview

Artificial Successes

Superficial Matches

Collective Transport

Swarm Assembly

New Hopes

Conclusions



Collective Transport

Decentralized Organization of *Ant* Teams Carrying Loads

Overview

Artificial Successes

Superficial Matches

Collective Transport

Swarm Assembly

New Hopes

Conclusions



Possible Extension: Swarm Robotic Assembly

(Matthey et al. 2009)

Overview

Artificial Successes

Superficial Matches

Collective Transport

Swarm Assembly

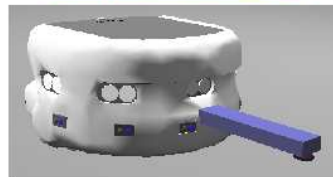
New Hopes

Conclusions

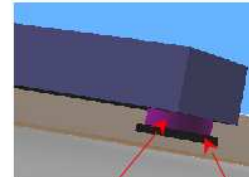
Stochastic Strategies for a Swarm Robotic Assembly System

Loïc Matthey, Spring Berman and Vijay Kumar

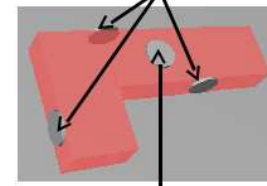
Khepera III + bar
(www.k-team.com)



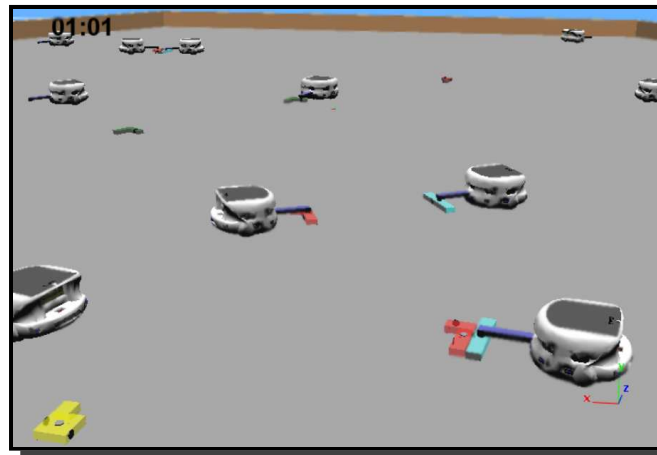
Rotational servo Magnet



Magnets that bond to other parts



Bonds to bar



Possible Extension: Swarm Robotic Assembly

(Matthey et al. 2009)

Overview

Artificial Successes

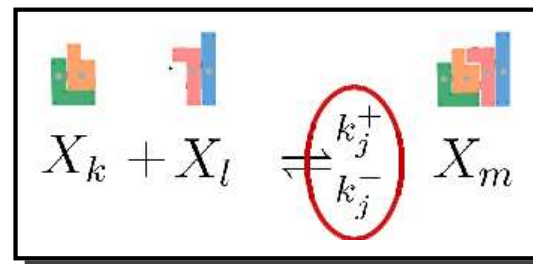
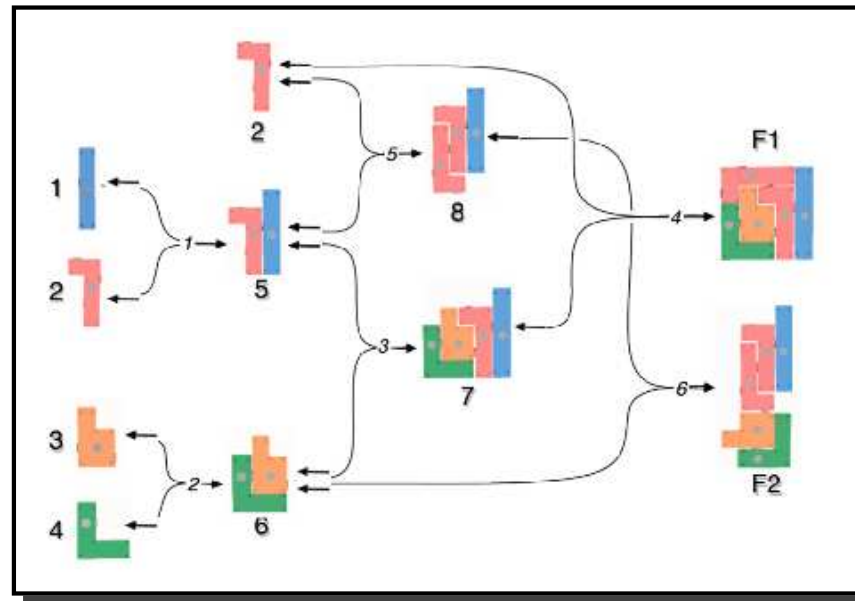
Superficial Matches

Collective Transport

Swarm Assembly

New Hopes

Conclusions



Goal: Regulate ratio of assembled parts at equilibrium (e.g., $x_{F1}^* = 2x_{F2}^*$).

Possible Extension: Honeycomb Assembly?

(Seeley and Morse 1976; Pratt 2004; Cargel and Rinderer 2004; Livnat and Pippenger 2006)

Overview

Artificial Successes

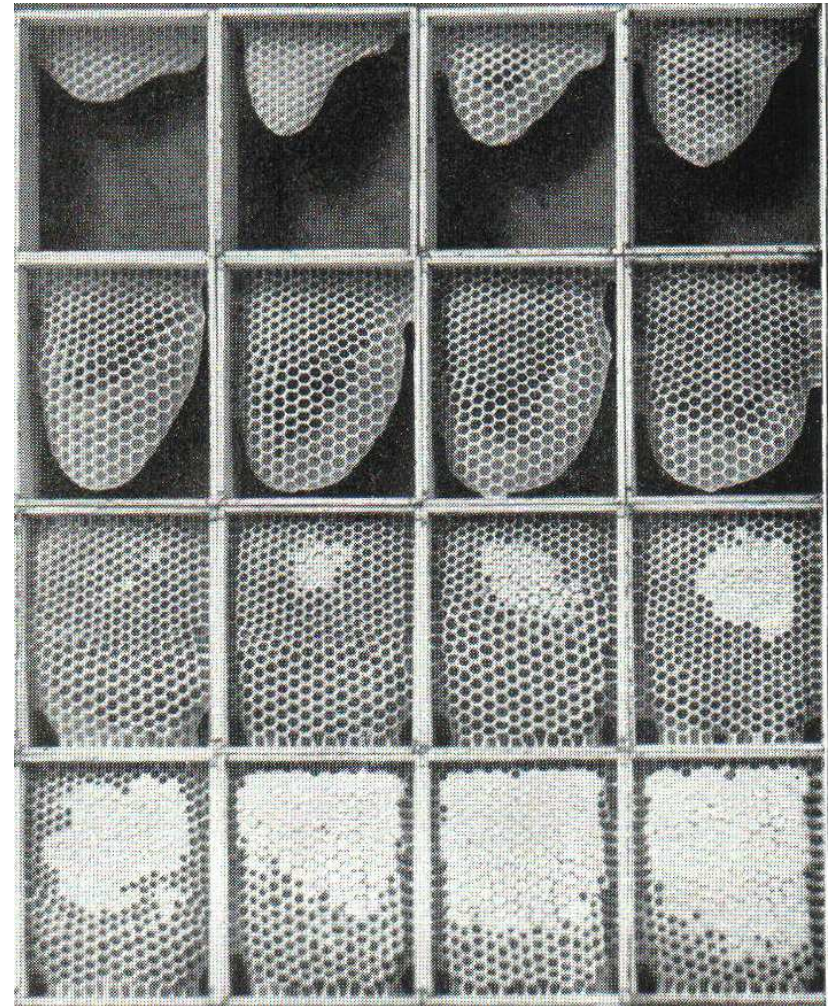
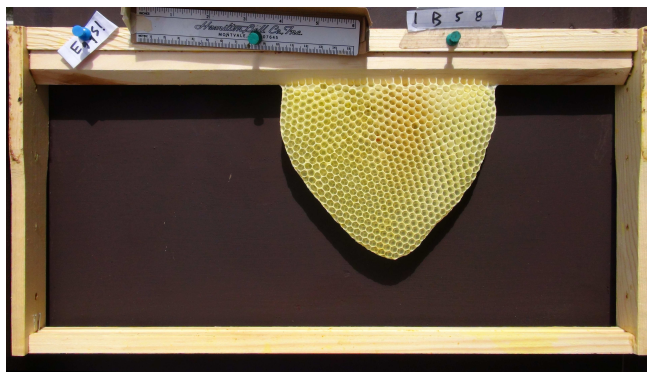
Superficial Matches

Collective Transport

Swarm Assembly

New Hopes

Conclusions



Stochastic Assembly in Honeybee Colonies

A Simple Model

Overview

Artificial Successes

Superficial Matches

Collective Transport

Swarm Assembly

New Hopes

Conclusions

Worker + Earlier Cell $\xrightarrow{p_b e_c}$ Worker + Later Cell

Worker + Later Cell $\xrightarrow{p_u e_c}$ Worker + Earlier Cell

Active Cell $\xrightarrow{\text{SLOW}}$ Finished Cell

Stochastic Assembly in Honeybee Colonies

A Simple Model

Overview

Artificial Successes

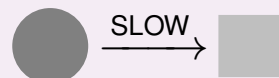
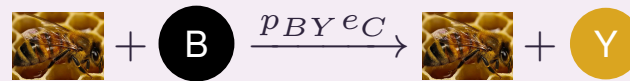
Superficial Matches

Collective Transport

Swarm Assembly

New Hopes

Conclusions



Stochastic Assembly in Honeybee Colonies

A Simple Model

Overview

Artificial Successes

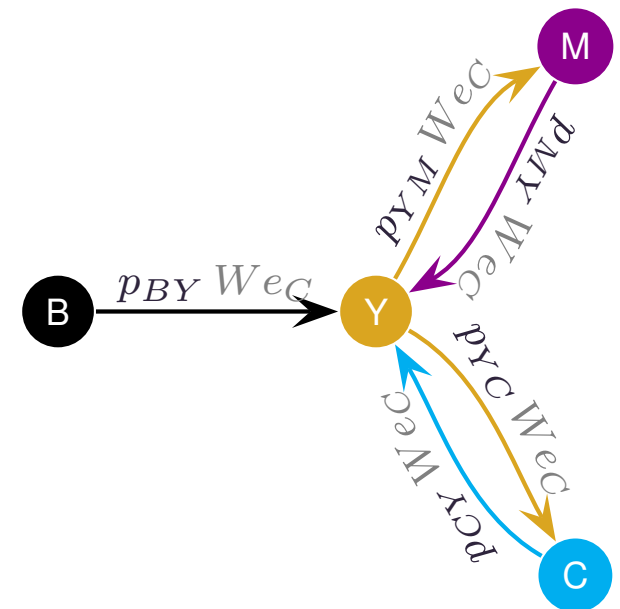
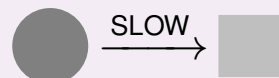
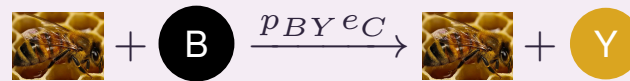
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Collective Transport

Swarm Assembly

New Hopes

Conclusions



Stochastic Assembly in Honeybee Colonies

A Simple Model

Overview

Artificial Successes

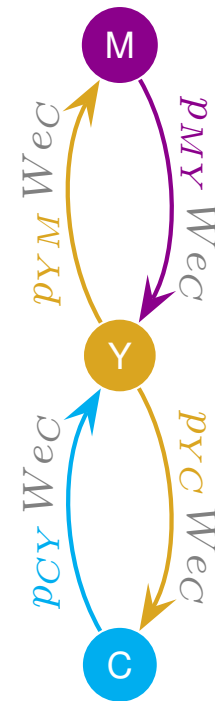
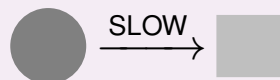
Superficial Matches

Collective Transport

Swarm Assembly

New Hopes

Conclusions



Stochastic Assembly in Honeybee Colonies

A Simple Model

Overview

Artificial Successes

Superficial Matches

Collective Transport

Swarm Assembly

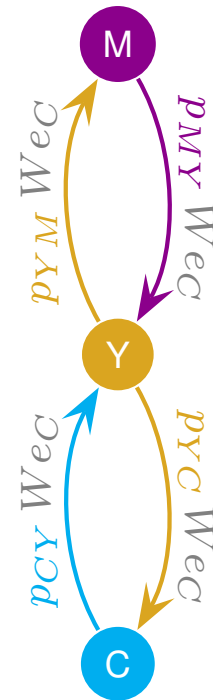
New Hopes

Conclusions

$$Y p_{YM} - M p_{MY} = 0$$

$$Y p_{YC} - C p_{CY} = 0$$

$$Y + M + C = 1$$



Stochastic Assembly in Honeybee Colonies

A Simple Model

Overview

Artificial Successes

Superficial Matches

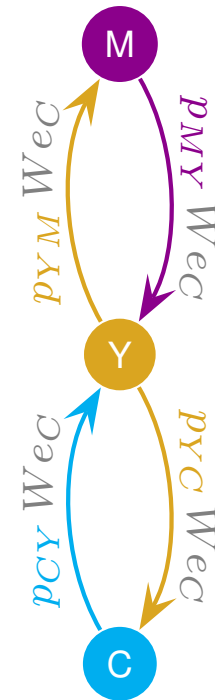
Collective Transport

Swarm Assembly

New Hopes

Conclusions

$$\begin{bmatrix} Y \\ M \\ C \end{bmatrix} = \frac{\begin{bmatrix} pMYpCY \\ pYMP CY \\ pMYpYC \end{bmatrix}}{pYMP CY + pMYpYC + pMYpCY}$$



Stochastic Assembly in Honeybee Colonies

A Simple Model

Overview

Artificial Successes

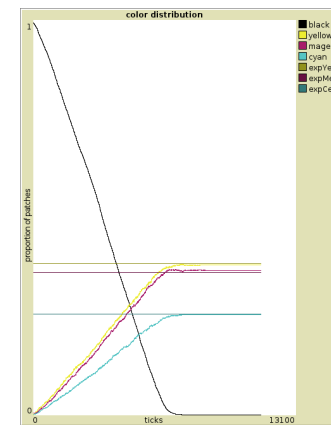
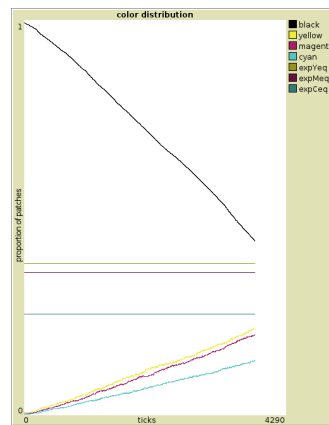
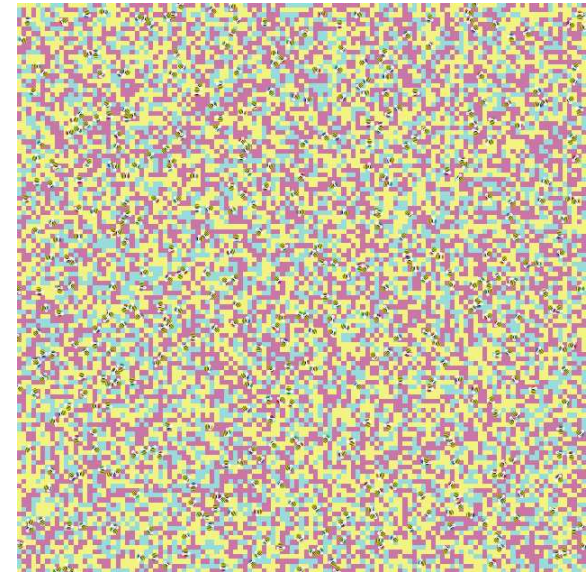
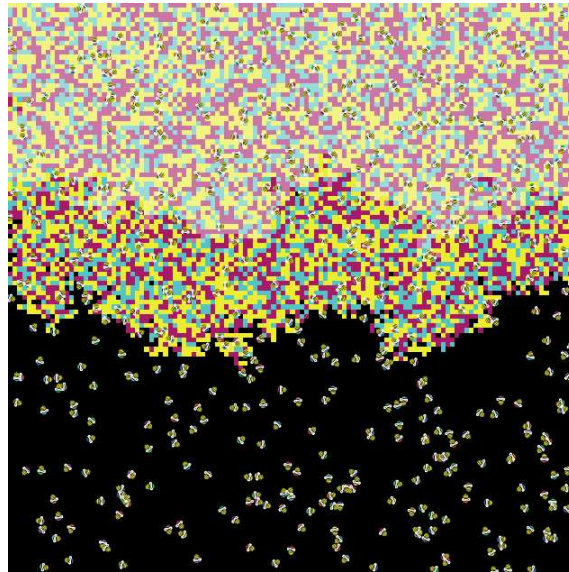
Superficial Matches

Collective Transport

Swarm Assembly

New Hopes

Conclusions



Stochastic Assembly in Honeybee Colonies

A Simplistic Model

Overview

Artificial Successes

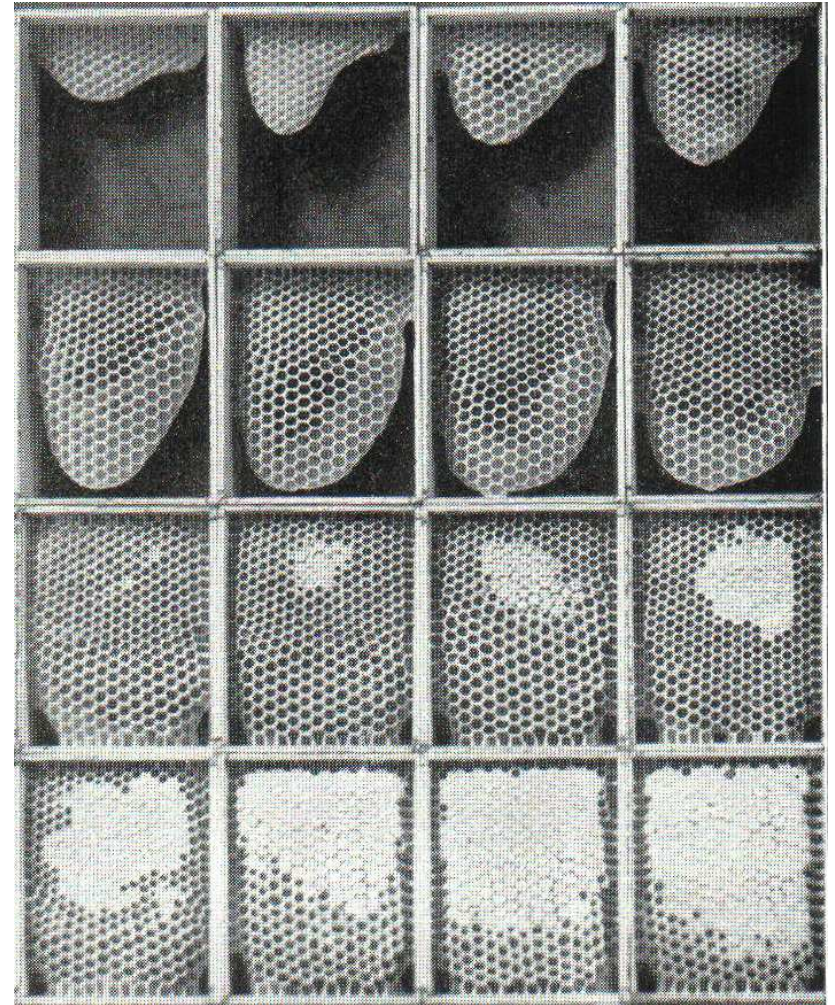
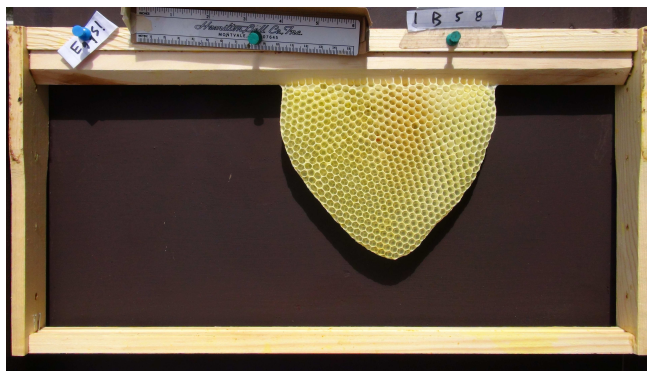
Superficial Matches

Collective Transport

Swarm Assembly

New Hopes

Conclusions



Temnothorax nest-site selection

Overview

Artificial Successes

Superficial Matches

New Hopes

Drift-Diffusion
Decision-Making

Conclusions

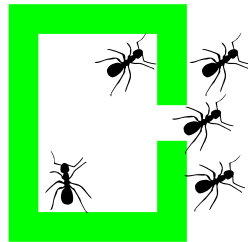


Photo: Takao Sasaki, James S. Waters

Temnothorax nest-site selection

Overview

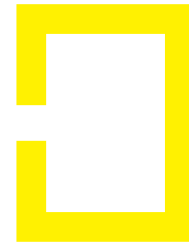
Artificial Successes

Superficial Matches

New Hopes

Drift-Diffusion
Decision-Making

Conclusions



Temnothorax nest-site selection

Overview

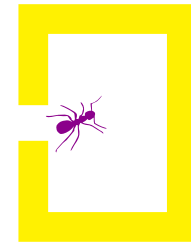
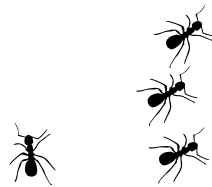
Artificial Successes

Superficial Matches

New Hopes

Drift-Diffusion
Decision-Making

Conclusions



Temnothorax nest-site selection

Overview

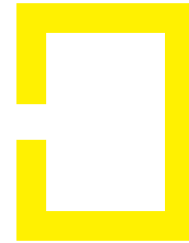
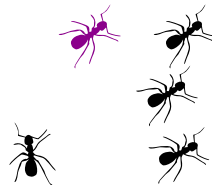
Artificial Successes

Superficial Matches

New Hopes

Drift-Diffusion
Decision-Making

Conclusions



Temnothorax nest-site selection

Overview

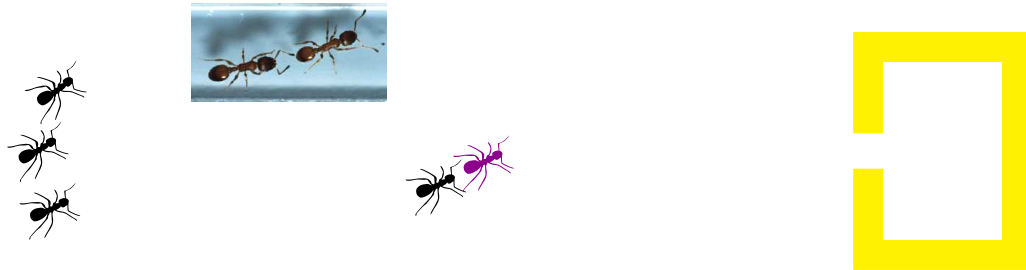
Artificial Successes

Superficial Matches

New Hopes

Drift-Diffusion
Decision-Making

Conclusions



“Tandem run”

Slow transit, but adds one more recruiter.

Temnothorax nest-site selection

Overview

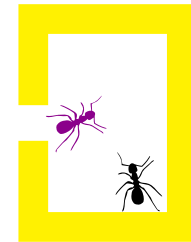
Artificial Successes

Superficial Matches

New Hopes

Drift-Diffusion
Decision-Making

Conclusions



Temnothorax nest-site selection

Overview

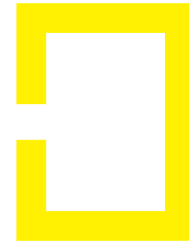
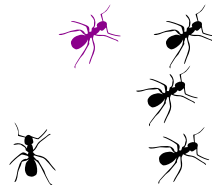
Artificial Successes

Superficial Matches

New Hopes

Drift-Diffusion
Decision-Making

Conclusions



Temnothorax nest-site selection

Overview

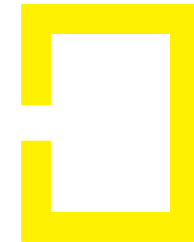
Artificial Successes

Superficial Matches

New Hopes

Drift-Diffusion
Decision-Making

Conclusions



“Transport”

Fast transit, but no additional recruiter.

Temnothorax nest-site selection

Overview

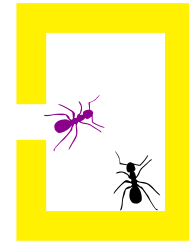
Artificial Successes

Superficial Matches

New Hopes

Drift-Diffusion
Decision-Making

Conclusions



Temnothorax nest-site selection

Overview

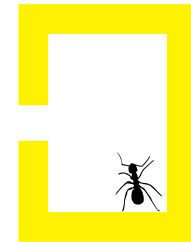
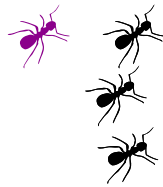
Artificial Successes

Superficial Matches

New Hopes

Drift-Diffusion
Decision-Making

Conclusions



Temnothorax nest-site selection

Overview

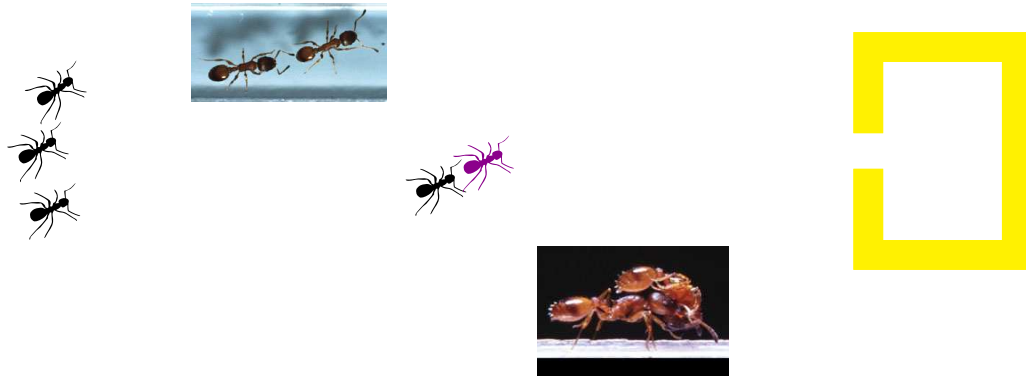
Artificial Successes

Superficial Matches

New Hopes

Drift-Diffusion
Decision-Making

Conclusions

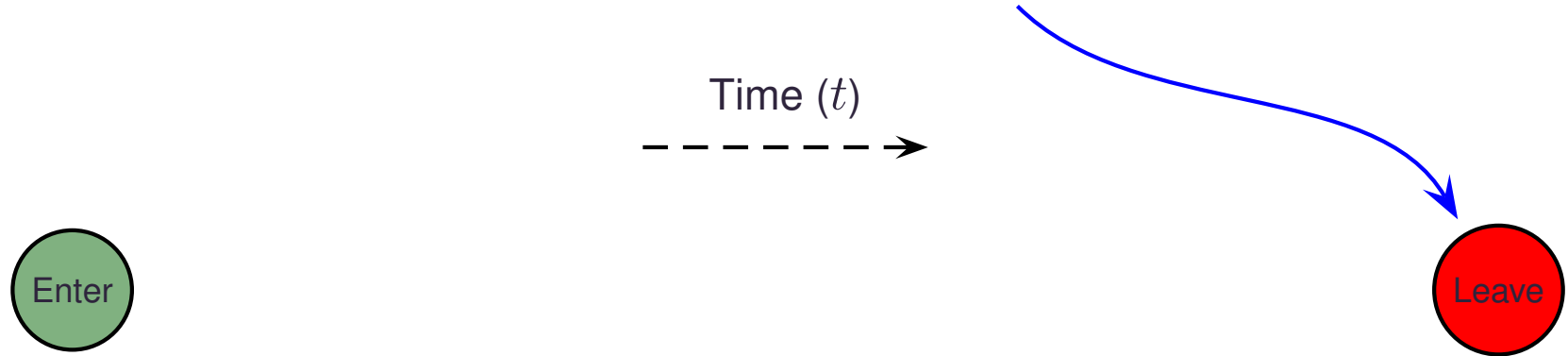


When to switch?

Recruitment decision process

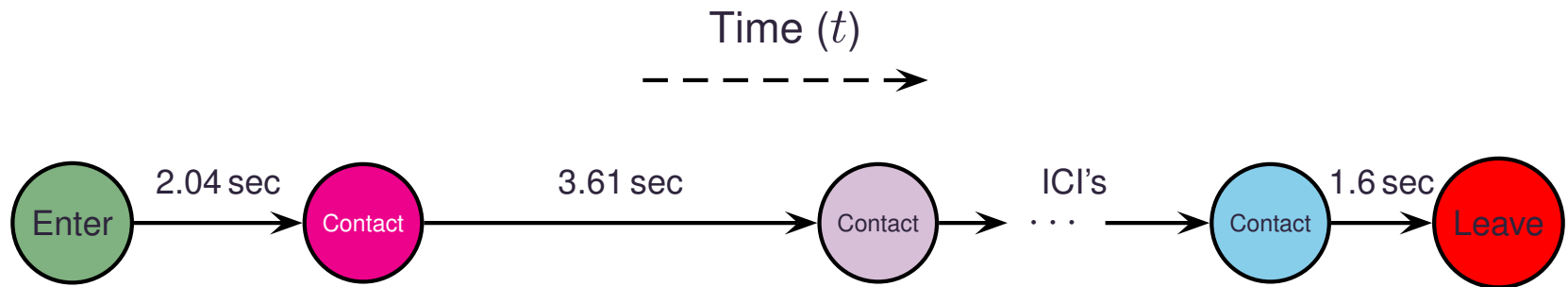
- Overview
- Artificial Successes
- Superficial Matches
- New Hopes
 - Drift-Diffusion
 - Decision-Making
- Conclusions

Inside the nest (immediately prior to a tandem-run or transport decision):



Recruitment decision process

Inside the nest (immediately prior to a tandem-run or transport decision):



Overview

Artificial Successes

Superficial Matches

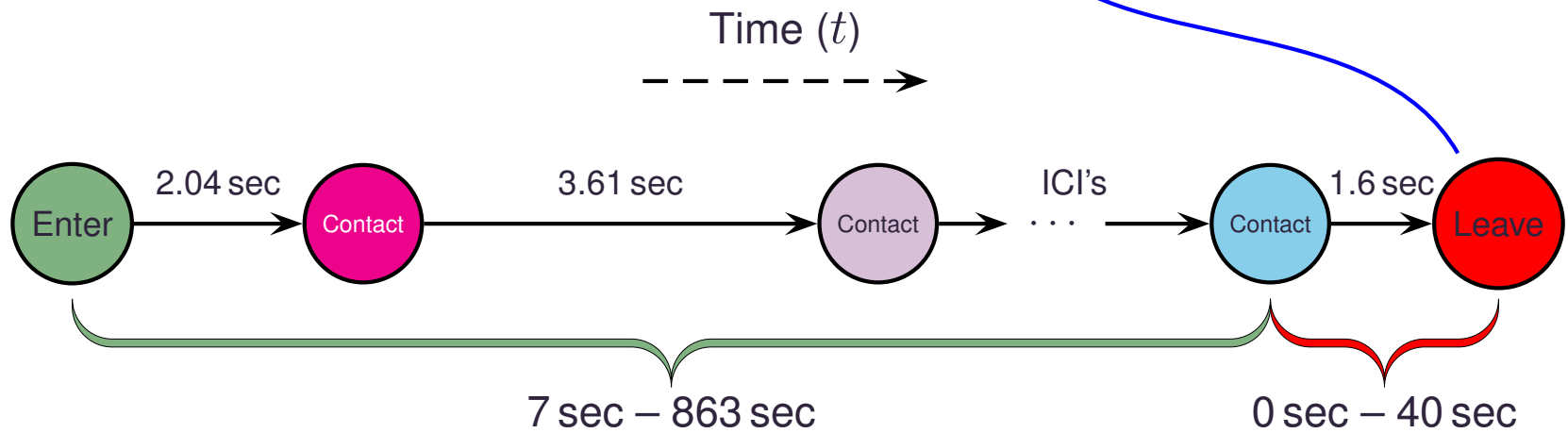
New Hopes

Drift-Diffusion
Decision-Making

Conclusions

Recruitment decision process

Inside the nest (immediately prior to a **tandem-run** or **transport decision**):



Overview

Artificial Successes

Superficial Matches

New Hopes

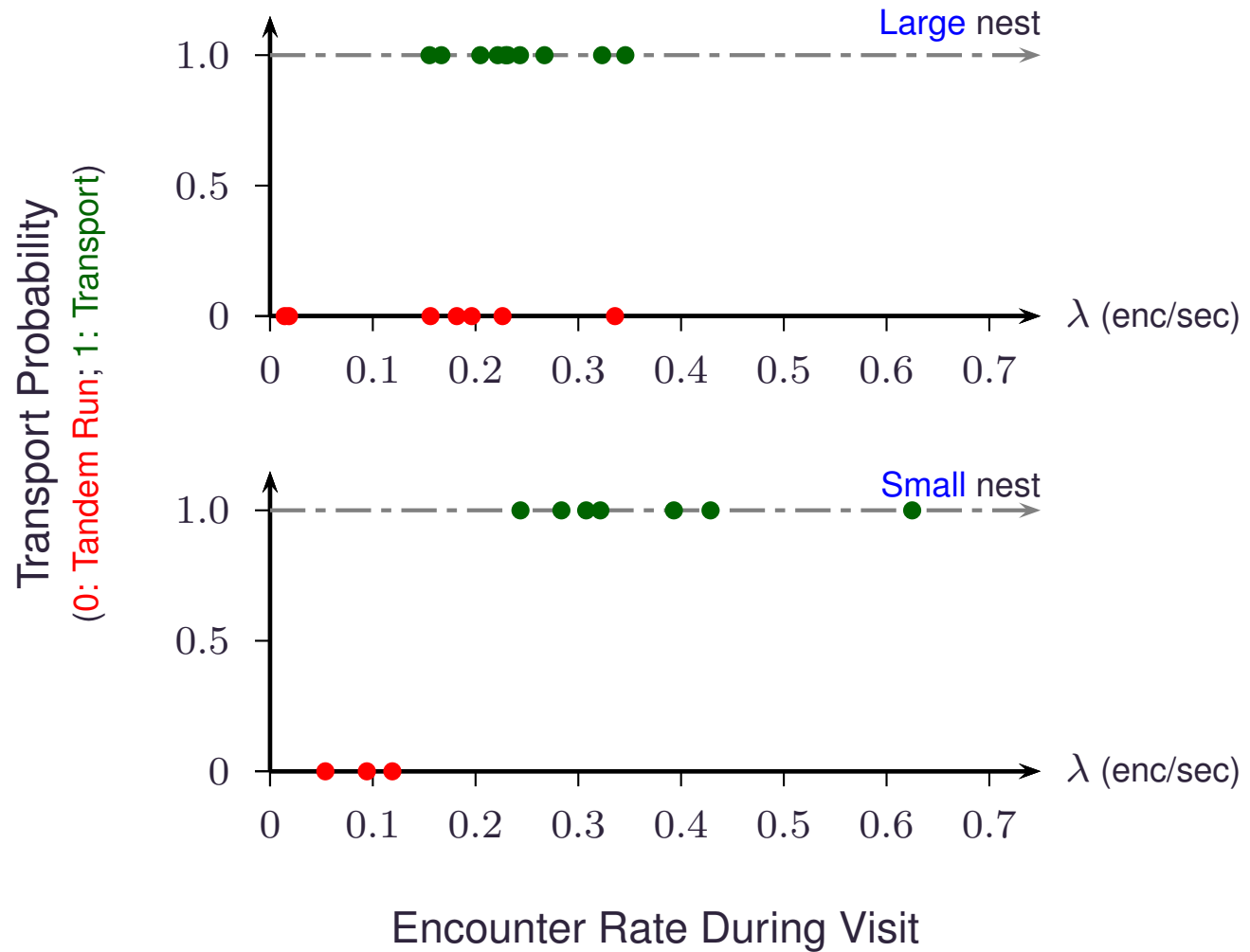
Drift-Diffusion
Decision-Making

Conclusions

Role of encounter rate

(Pratt 2005)

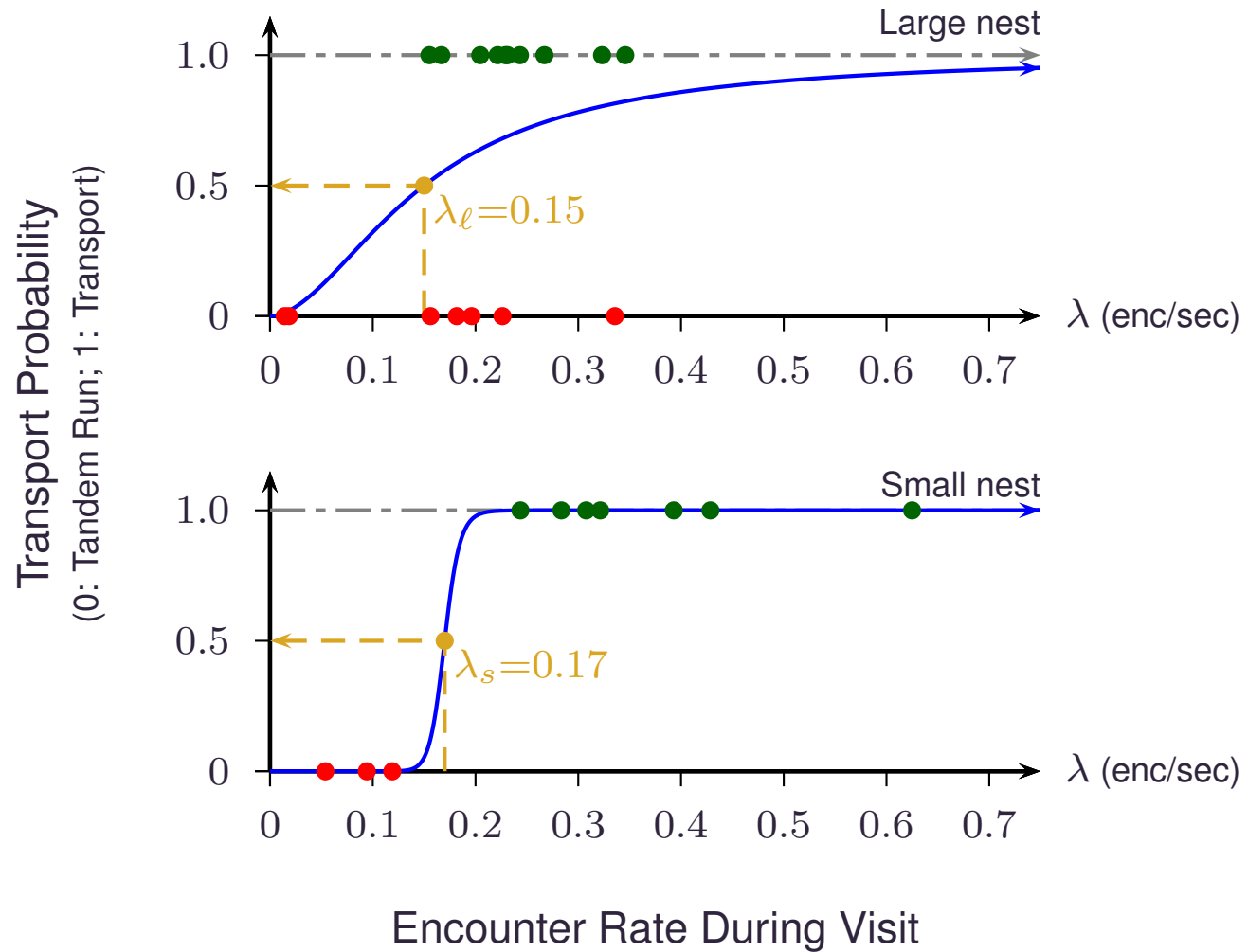
- Overview
- Artificial Successes
- Superficial Matches
- New Hopes
 - Drift-Diffusion
 - Decision-Making
- Conclusions



Role of encounter rate

(Pratt 2005)

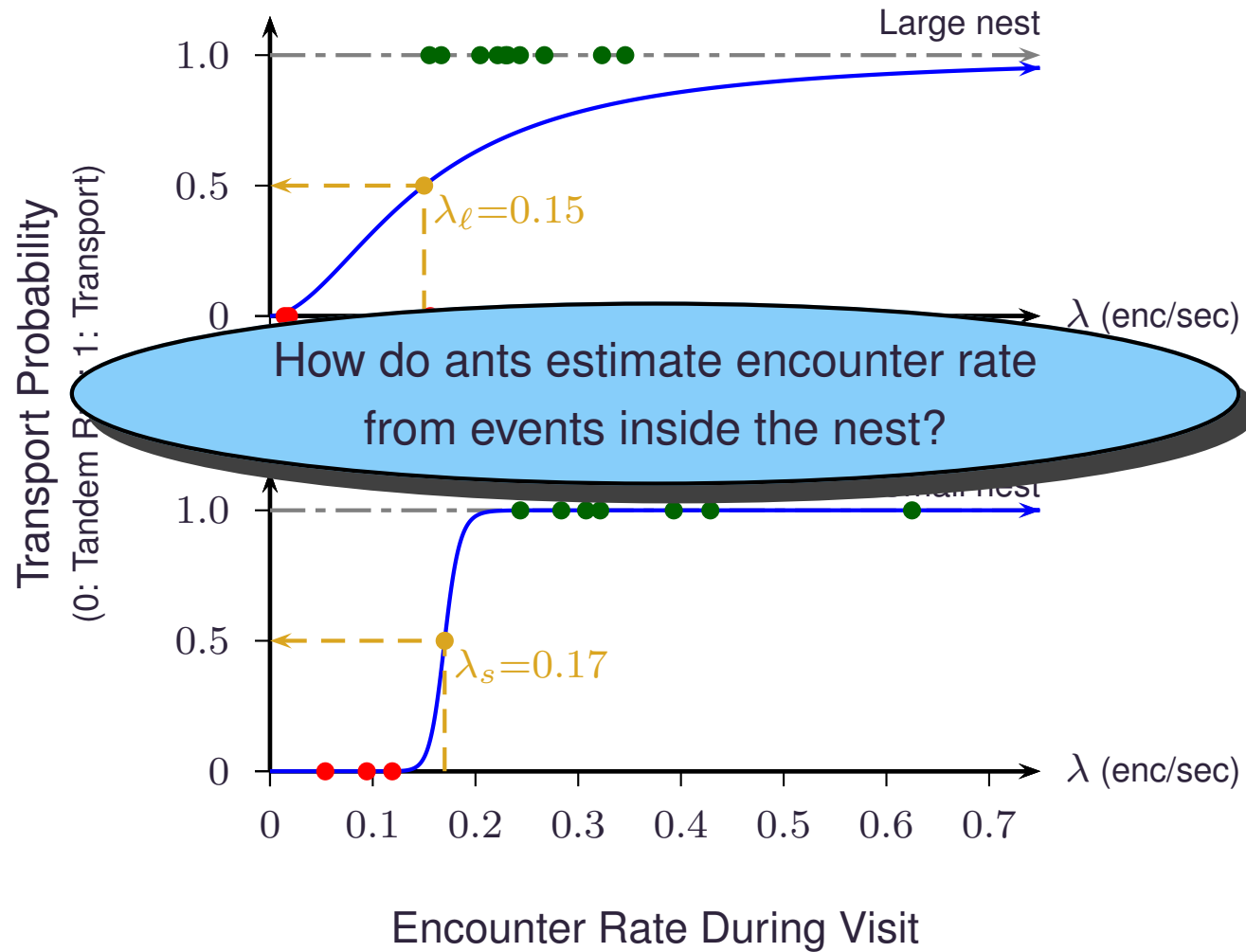
- Overview
- Artificial Successes
- Superficial Matches
- New Hopes
- Drift-Diffusion
Decision-Making
- Conclusions



Role of encounter rate

(Pratt 2005)

- Overview
- Artificial Successes
- Superficial Matches
- New Hopes
- Drift-Diffusion Decision-Making
- Conclusions



Encounter-rate detection and estimation?

Overview

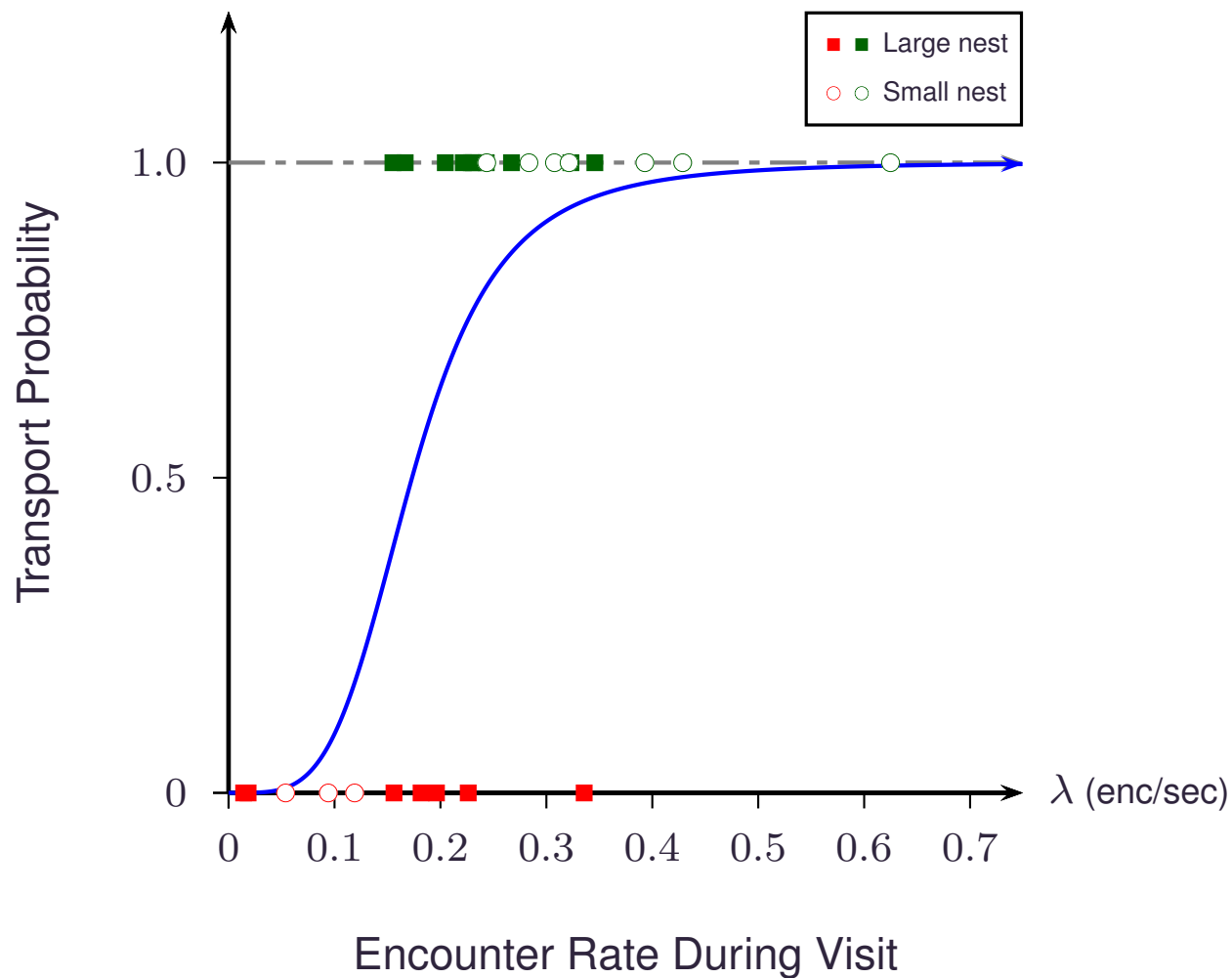
Artificial Successes

Superficial Matches

New Hopes

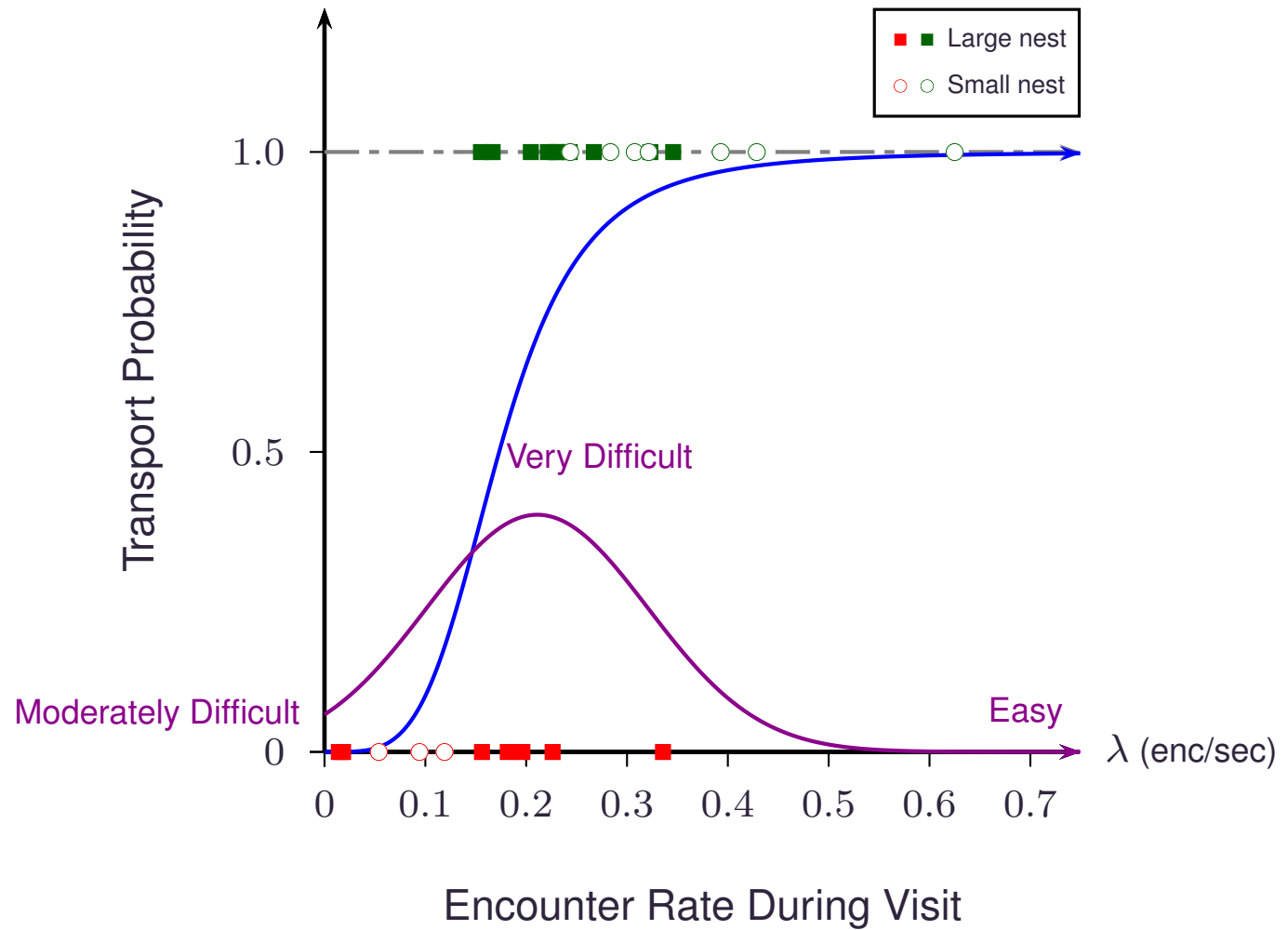
Drift-Diffusion
Decision-Making

Conclusions



Encounter-rate detection and estimation?

- Overview
- Artificial Successes
- Superficial Matches
- New Hopes
- Drift-Diffusion Decision-Making
- Conclusions



Encounter-rate detection and estimation?

Overview

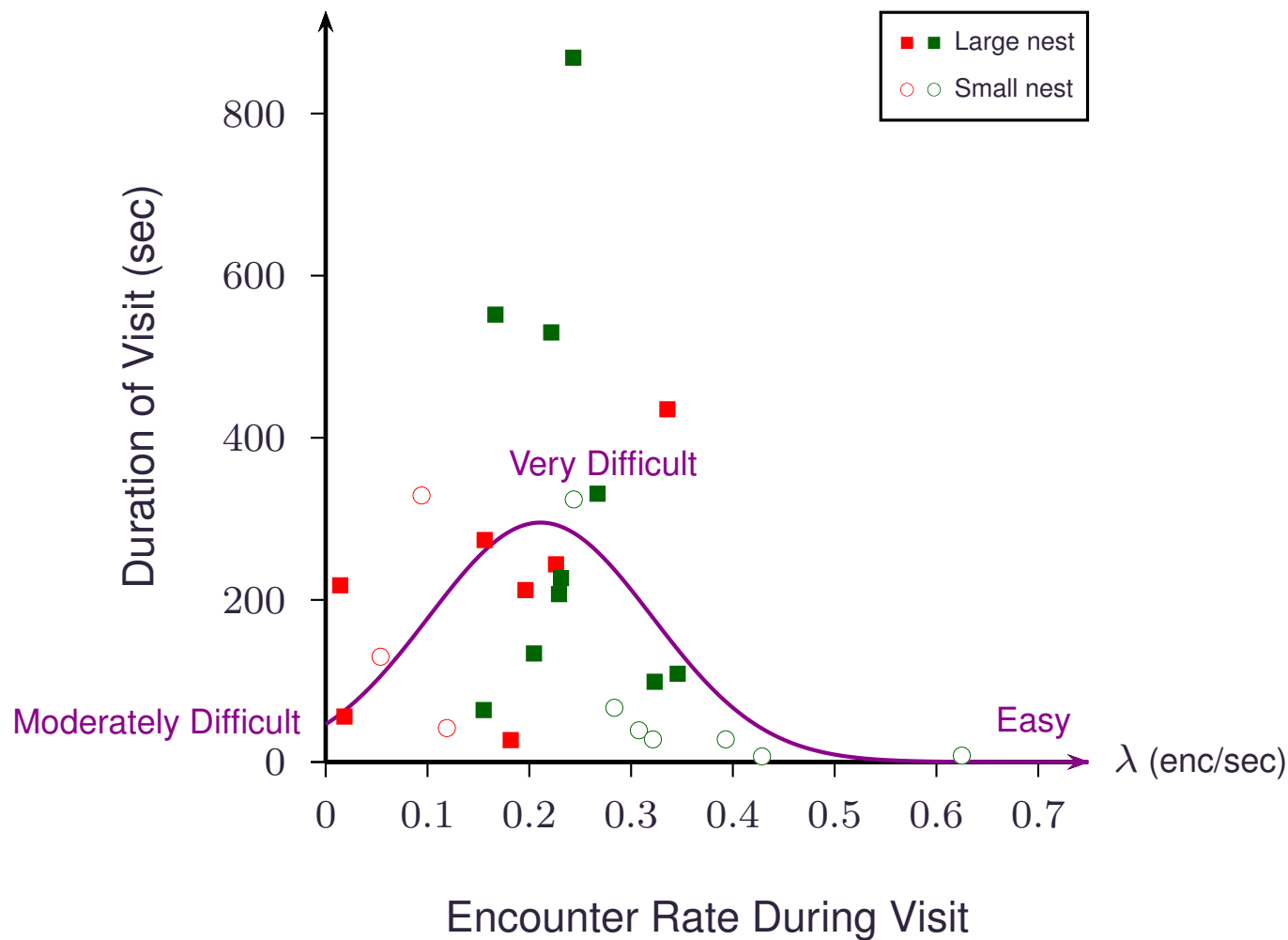
Artificial Successes

Superficial Matches

New Hopes

Drift-Diffusion
Decision-Making

Conclusions



Encounter-rate detection and estimation?

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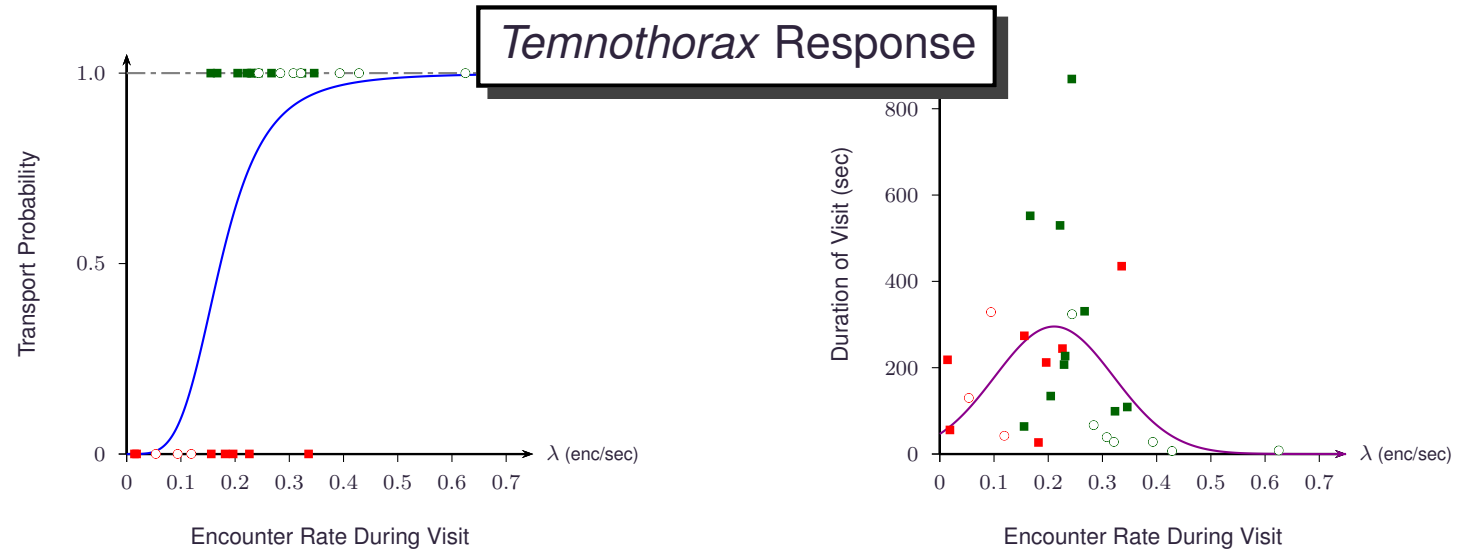
Artificial Successes

Superficial Matches

New Hopes

Drift-Diffusion
Decision-Making

Conclusions



Encounter-rate detection and estimation?

(Ratcliff et al. 1999)

Overview

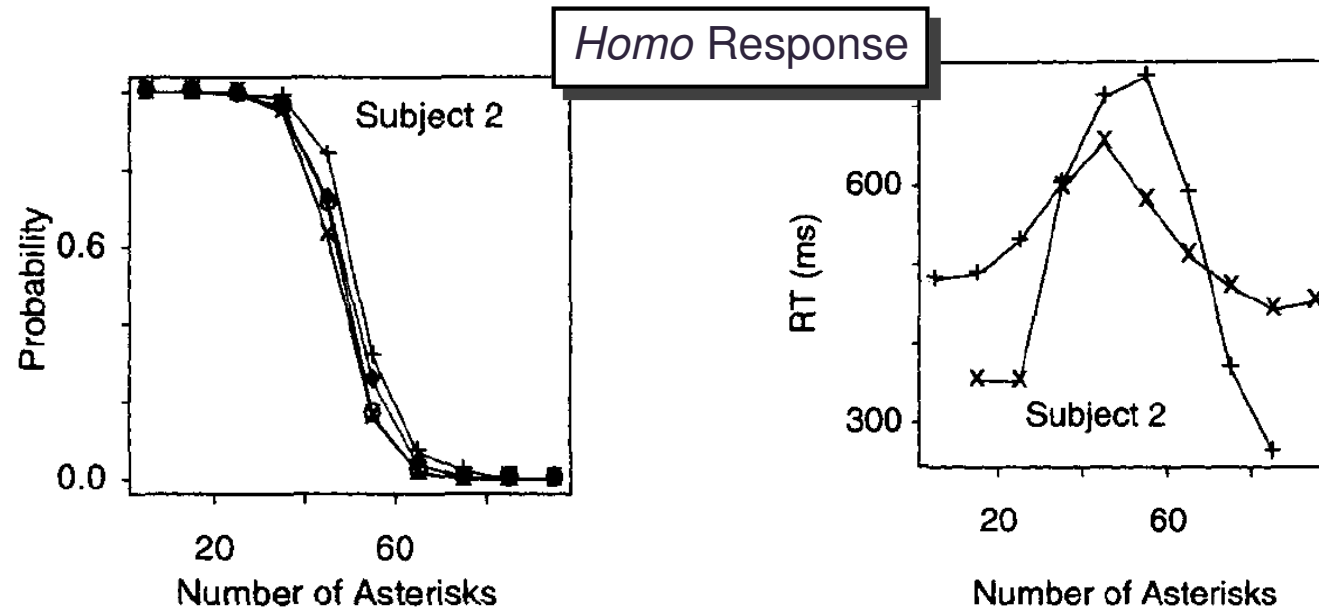
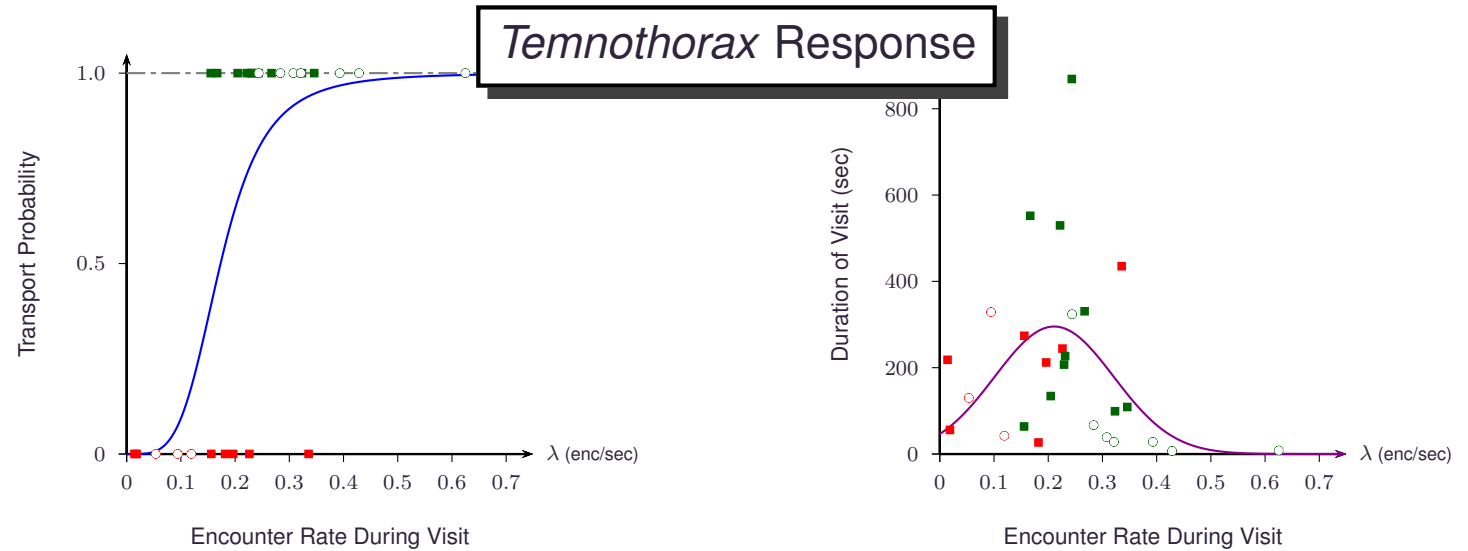
Artificial Successes

Superficial Matches

New Hopes

Drift-Diffusion
Decision-Making

Conclusions



Drift-diffusion model for two-choice tasks

(Ratcliff 1978; Ratcliff et al. 1999)

Overview

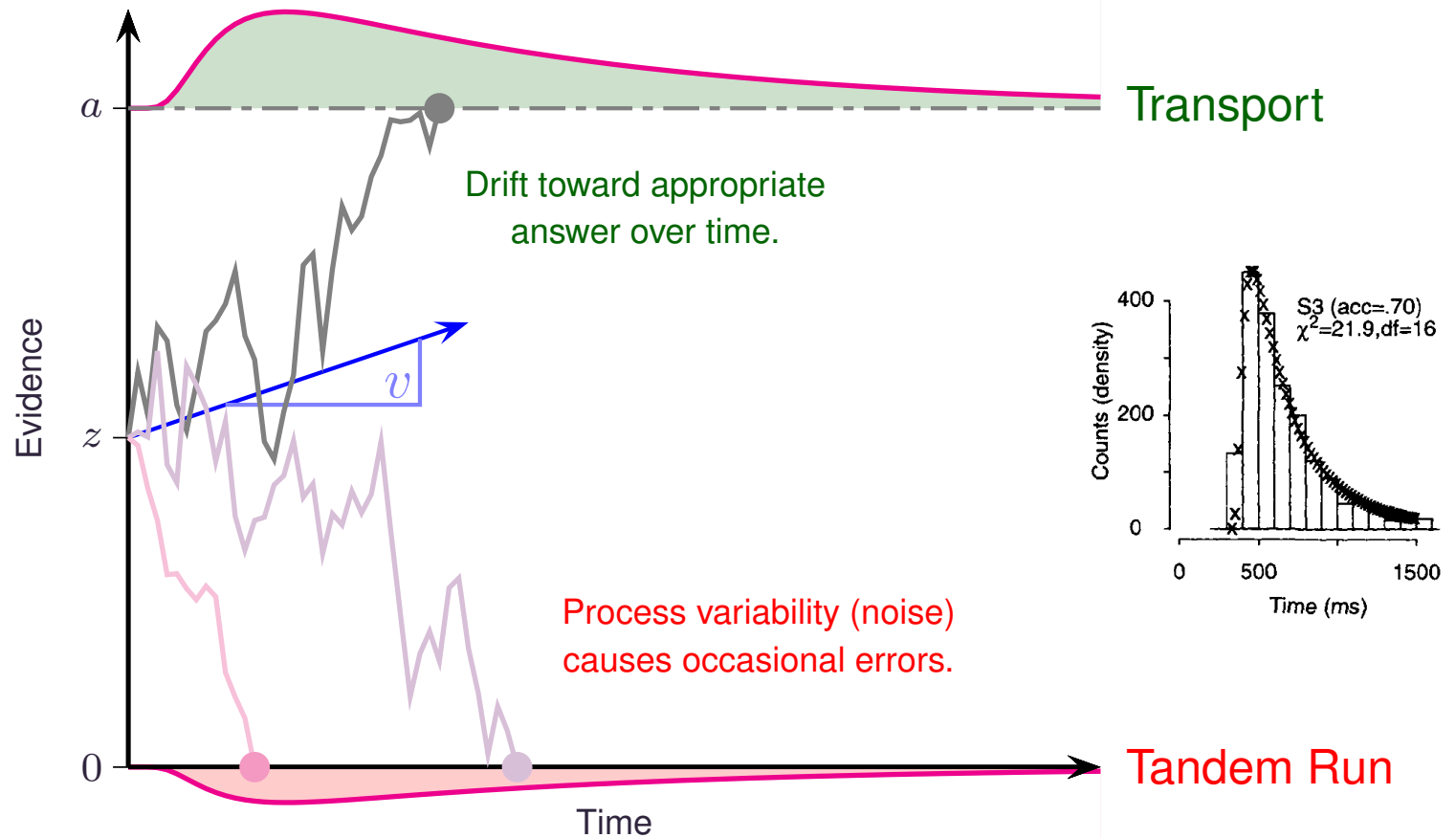
Artificial Successes

Superficial Matches

New Hopes

Drift-Diffusion
Decision-Making

Conclusions



Drift–diffusion model for quorum detection in *Temnothorax*

Overview

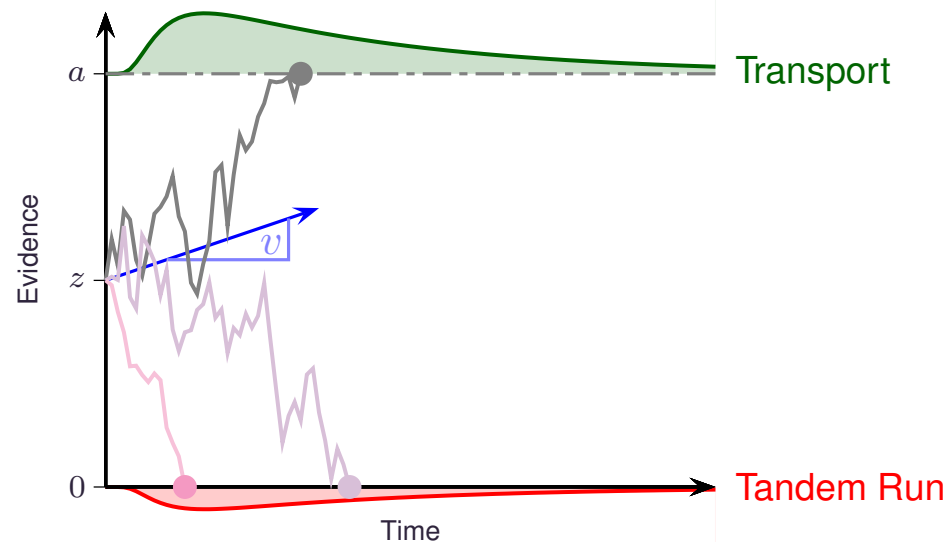
Artificial Successes

Superficial Matches

New Hopes

Drift–Diffusion
Decision-Making

Conclusions



■ Per-ant parameters of the model (generalized across sisters):

- a : Barrier separation (response time)
- z : Initial evidence variable (bias)
- T_{nd} : Non-decision time (actuation)
- λ_c : Critical encounter rate to detect

■ Model of condition-dependent confidence/difficulty

- $v \triangleq \lambda - \lambda_c$: Drift rate (λ measured from encounter data)

Drift–diffusion model for quorum detection in *Temnothorax*

Overview

Artificial Successes

Superficial Matches

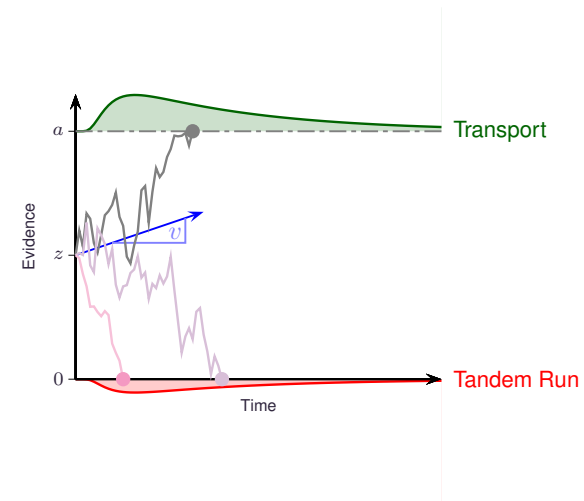
New Hopes

Drift–Diffusion
Decision-Making

Conclusions

■ Best-fit parameter results:

- $a = 26.729$
- $z = 8.0$
- $T_{nd} = 6.564 \text{ sec}$
- $\lambda_c = 0.173 \text{ enc/sec}$



Drift-diffusion model for quorum detection in *Temnothorax*

Overview

Artificial Successes

Superficial Matches

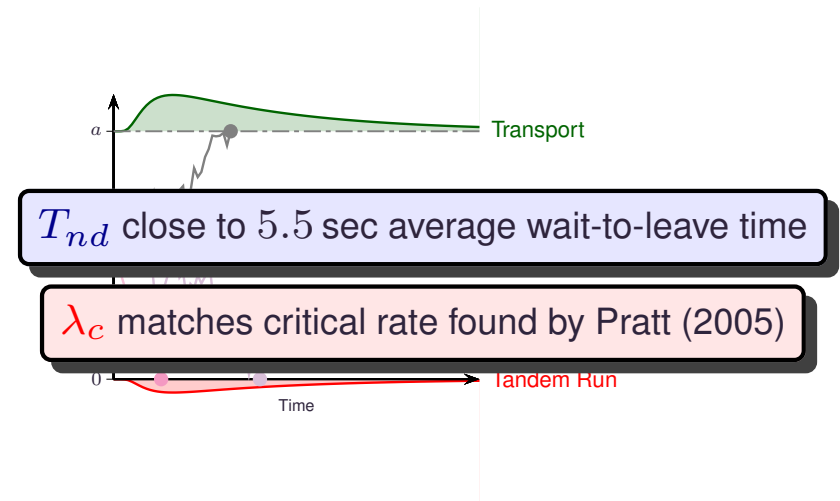
New Hopes

Drift-Diffusion
Decision-Making

Conclusions

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Drift-diffusion model for quorum detection in *Temnothorax*

- Overview

- Artificial Successes

- Superficial Matches

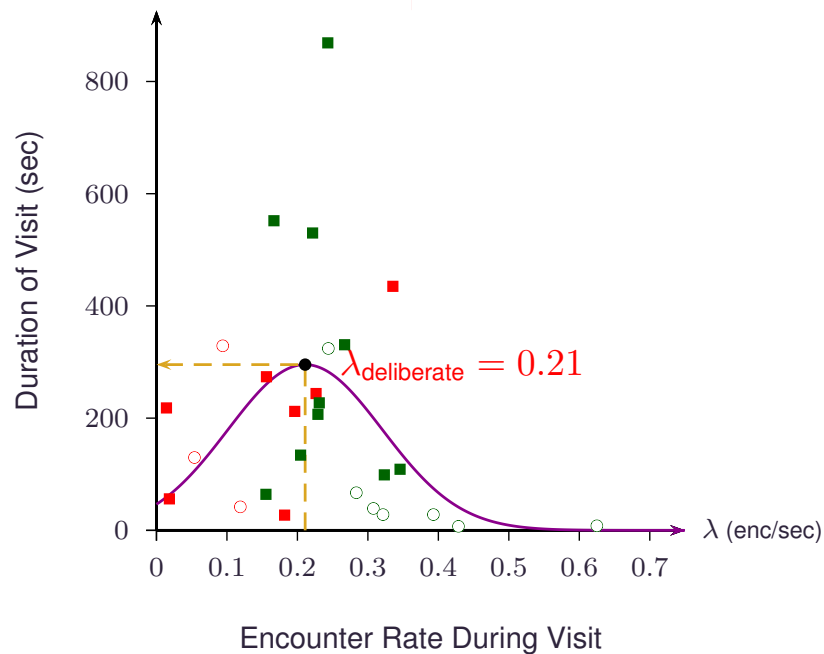
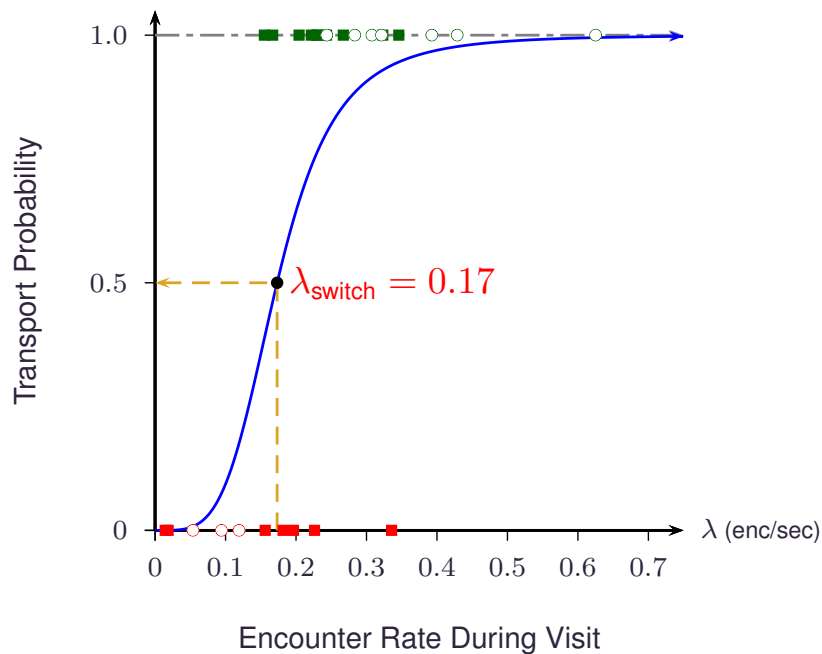
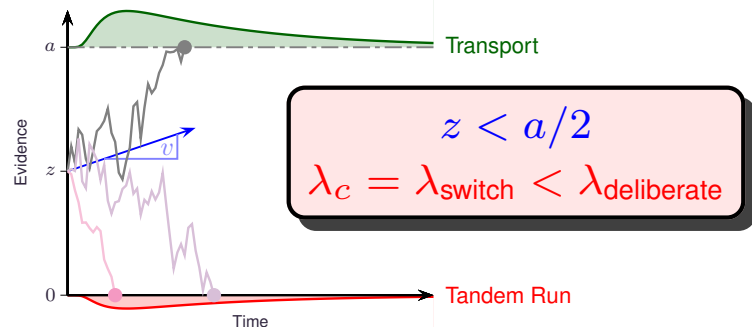
- New Hopes

- Drift-Diffusion
Decision-Making

- Conclusions

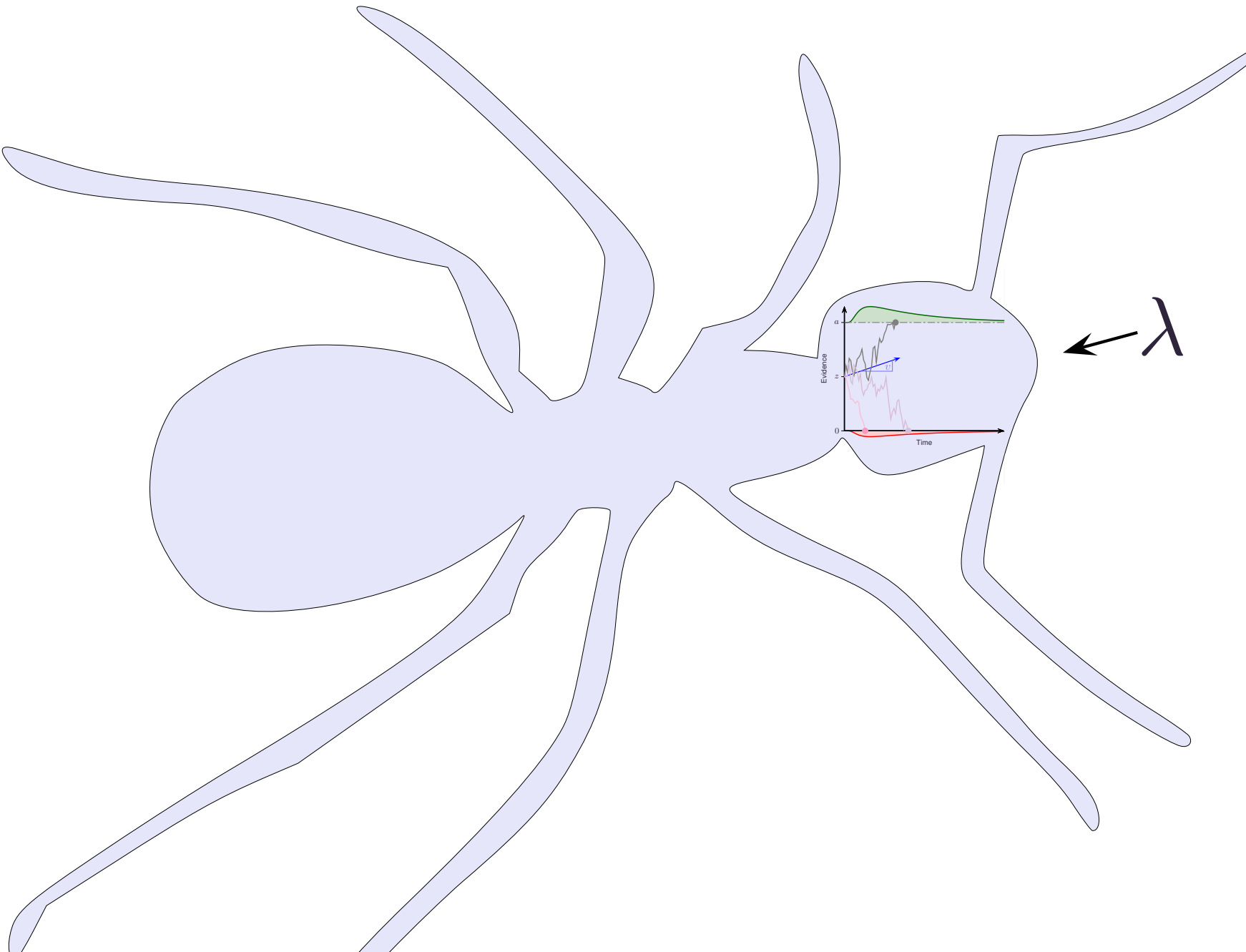
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Random walk: internal or external?

- Overview
- Artificial Successes
- Superficial Matches
- New Hopes
 - Drift-Diffusion
 - Decision-Making
- Conclusions



Random walk: internal or external?

Overview

Artificial Successes

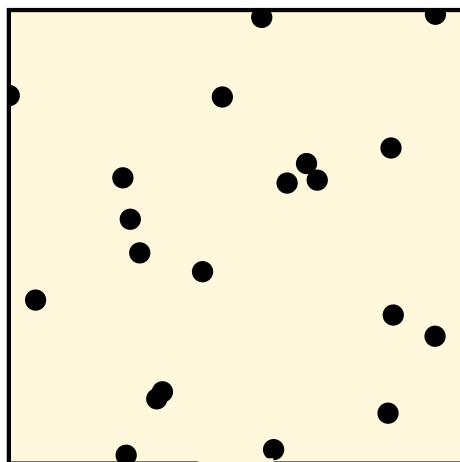
Superficial Matches

New Hopes

Drift-Diffusion
Decision-Making

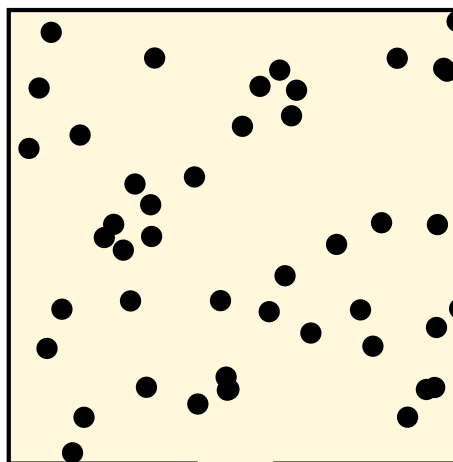
Conclusions

Tandem Run



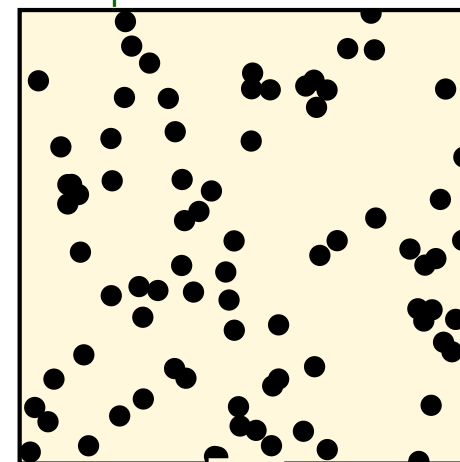
$\lambda = 0.1 \text{ enc/sec}$

No Preference

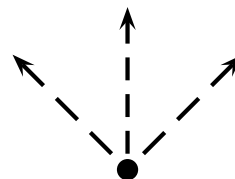


$\lambda = 0.24 \text{ enc/sec}$

Transport



$\lambda = 0.5 \text{ enc/sec}$



Recurrence time distributions?

Overview

Artificial Successes

Superficial Matches

New Hopes

Conclusions

- Coarse-graining introduces ambiguity
- Macroscopic consistencies can come about through multiple mechanisms

Overview

Artificial Successes

Superficial Matches

New Hopes

Conclusions

- Coarse-graining introduces ambiguity
- Macroscopic consistencies can come about through multiple mechanisms
- Simplest mechanisms are great candidates for engineering design
- Nature's adaptive mechanisms are constrained by phylogeny, ontogeny, and the environment (Tinbergen!)

Overview

Artificial Successes

Superficial Matches

New Hopes

Conclusions

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- Macroscopic consistencies can come about through multiple mechanisms
- Simplest mechanisms are great candidates for engineering design
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- Acknowledgments:
 - Spring M. Berman (ASU, SEMTE) + laboratory
 - Stephen C. Pratt (ASU, SOLS) + laboratory